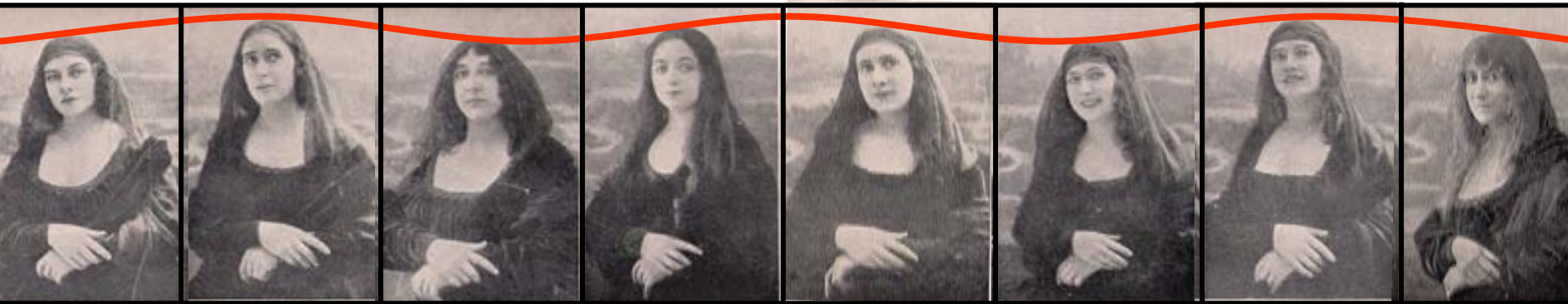




**LUND**  
UNIVERSITY

# Crystal Chemistry of Modulated Structures



# Disclaimer and copyright notice

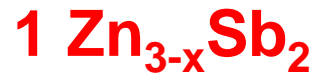
**Copyright 2010 Sven Lidin for this compilation.**

**This compilation is the collection of sheets of a presentation at the “International School on Aperiodic Crystals,” 26 September – 2 October 2010 in Carqueiranne, France. Reproduction or redistribution of this compilation or parts of it are not allowed.**

**This compilation may contain copyrighted material. The compilation may not contain complete references to sources of materials used in it. It is the responsibility of the reader to provide proper citations, if he or she refers to material in this compilation.**



# Examples

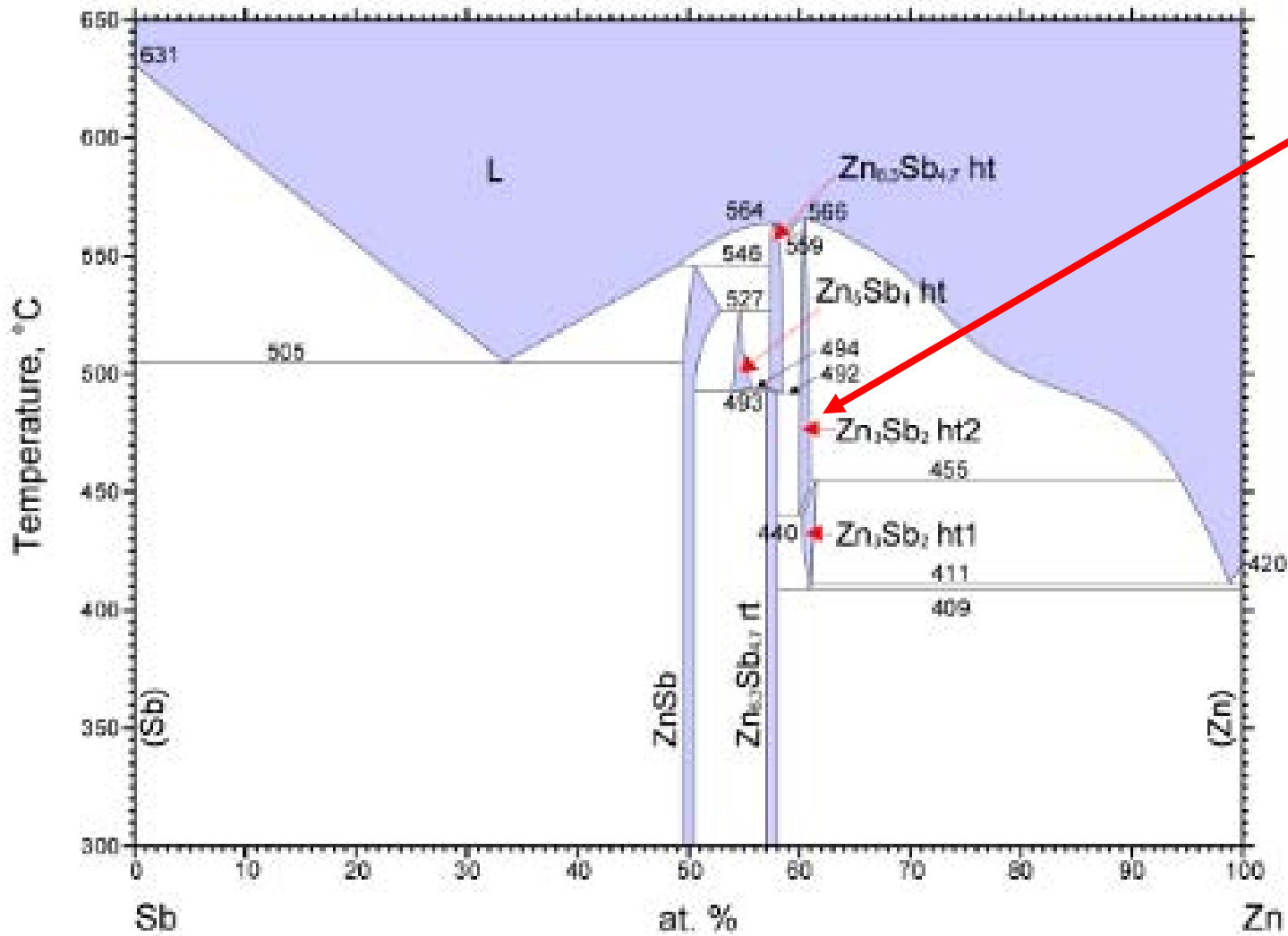


2 Stistaite

3 Onoratoite



# Zn<sub>3-x</sub>Sb<sub>2</sub>





# Modulated structure

Orthorhombic:

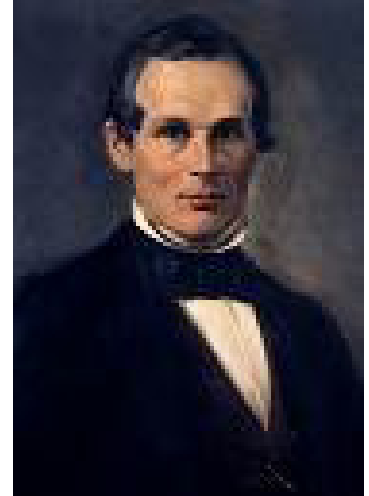
7.2834, 15.3976, 25.0555 Å →

$q \approx (0.385 \ 0 \ 0)$

$Pnaa(\alpha 00)0s0$

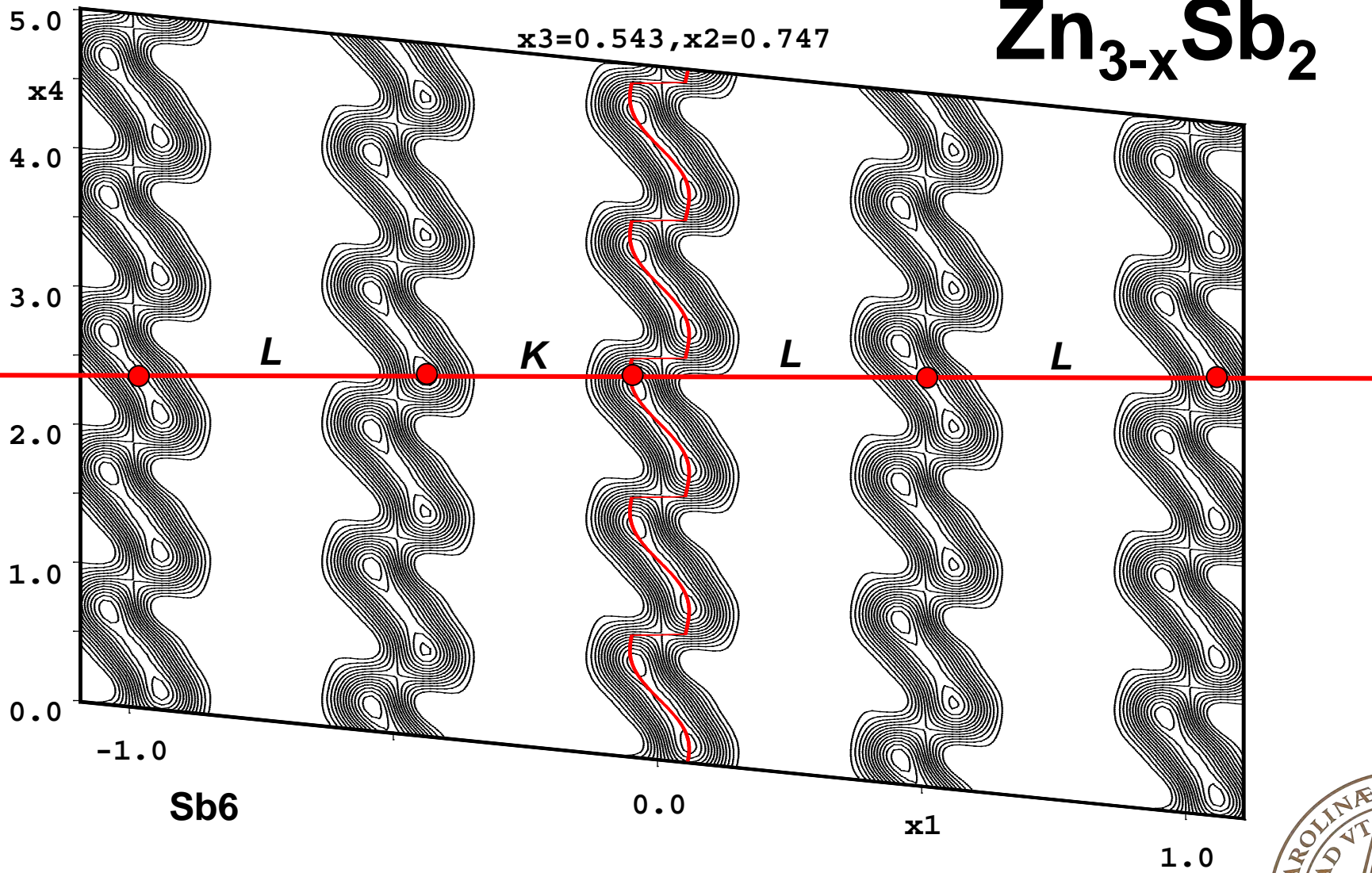
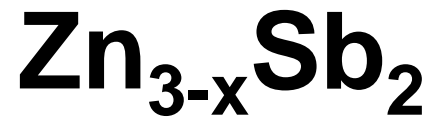
Five boring Sb positions, one exciting Sb  
Zn all over the place!

What is going on ?



**Anders Jöns Ångström**  
1814-1874







4.00

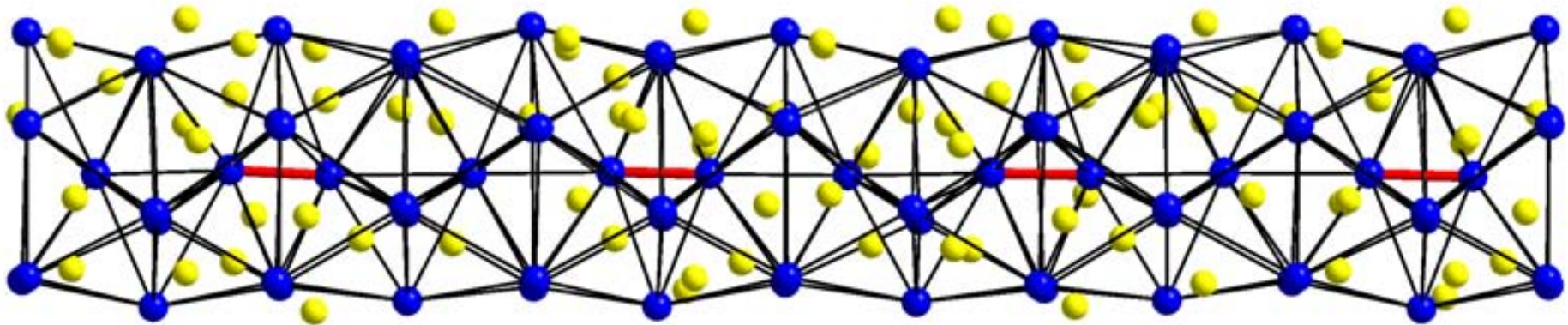
4.00

2.95

4.00

4.00

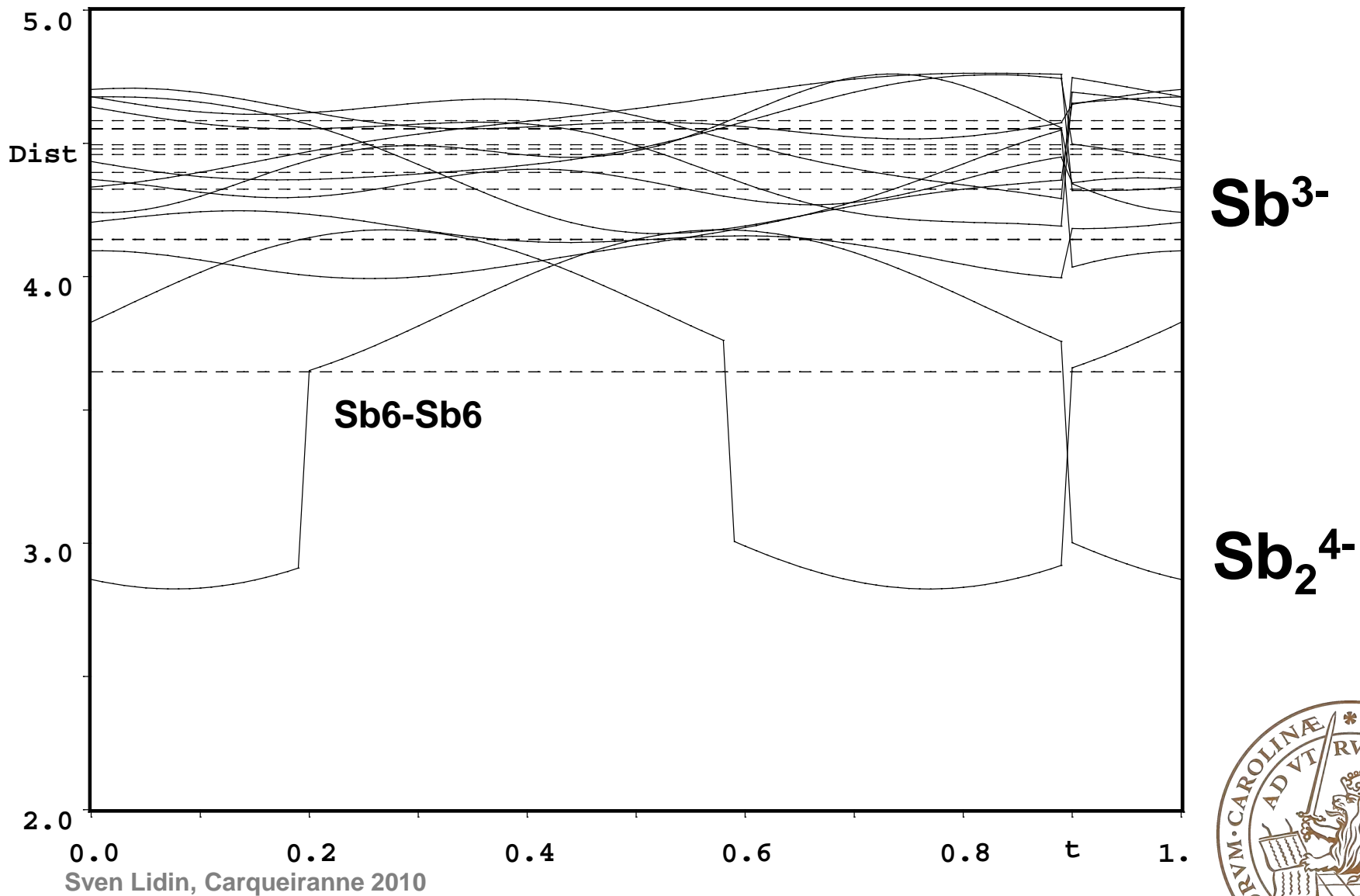
Å



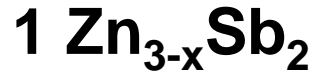
Zintl-pair formation in a pentagonal column



# Sb-Sb distances



# Examples

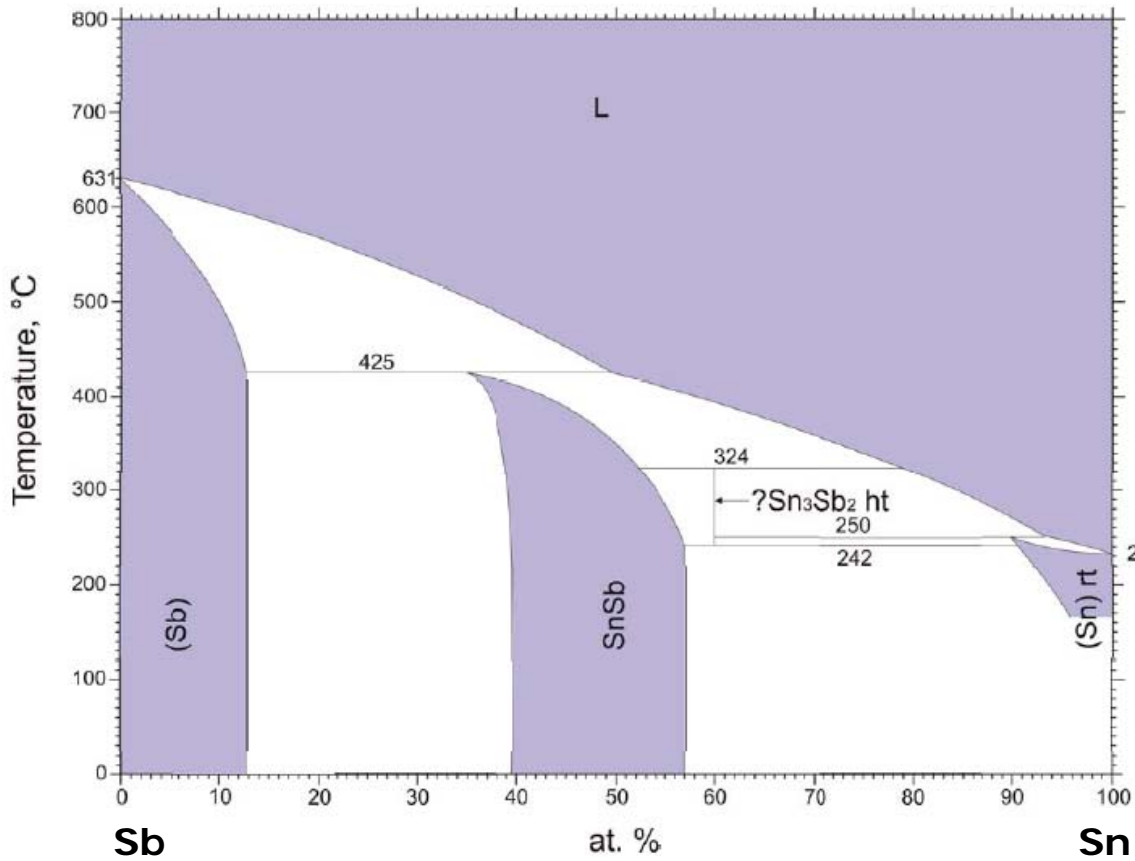


2 **Stistaite**

3 Onoratoite

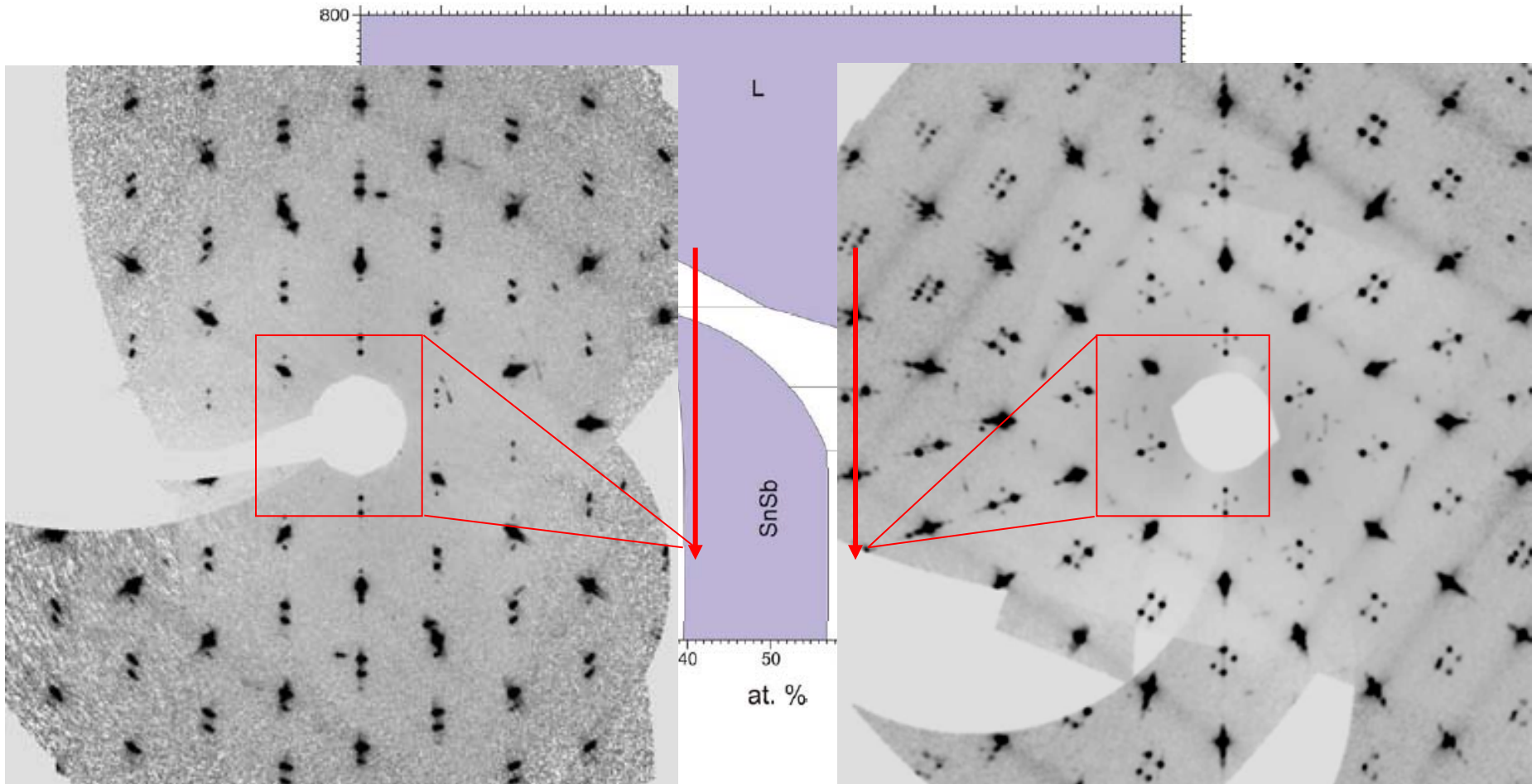


# How exciting is Sb-Sn?

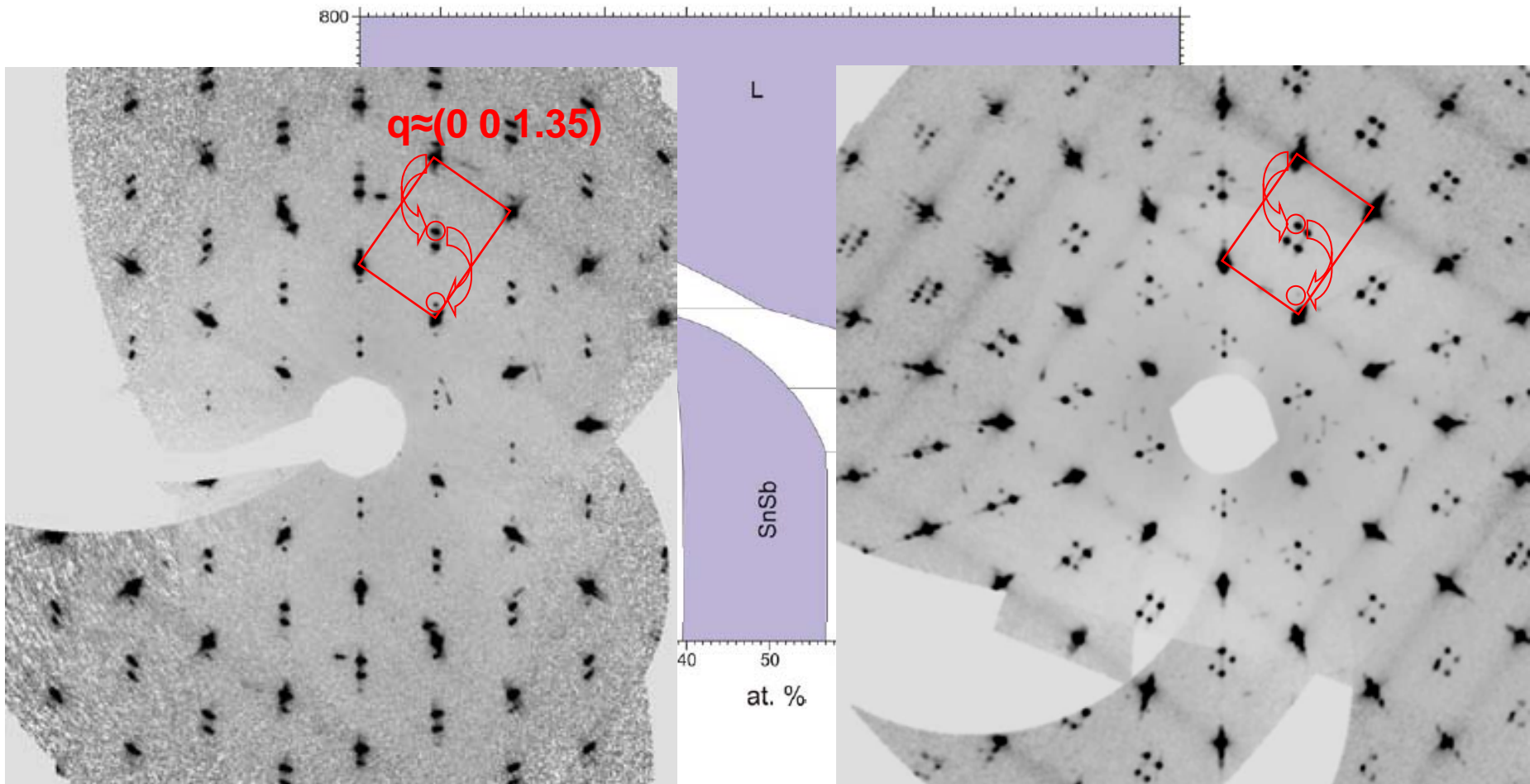




# Diffraction from Sb-Sn



# Diffraction from Sb-Sn

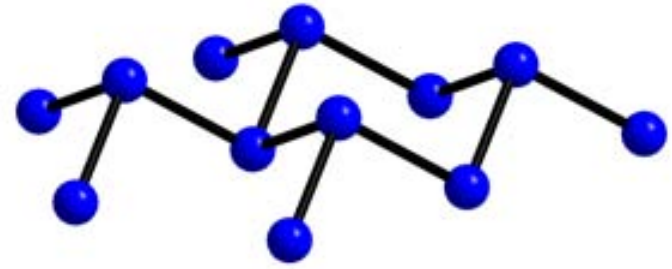




# Questions of crystal chemistry:

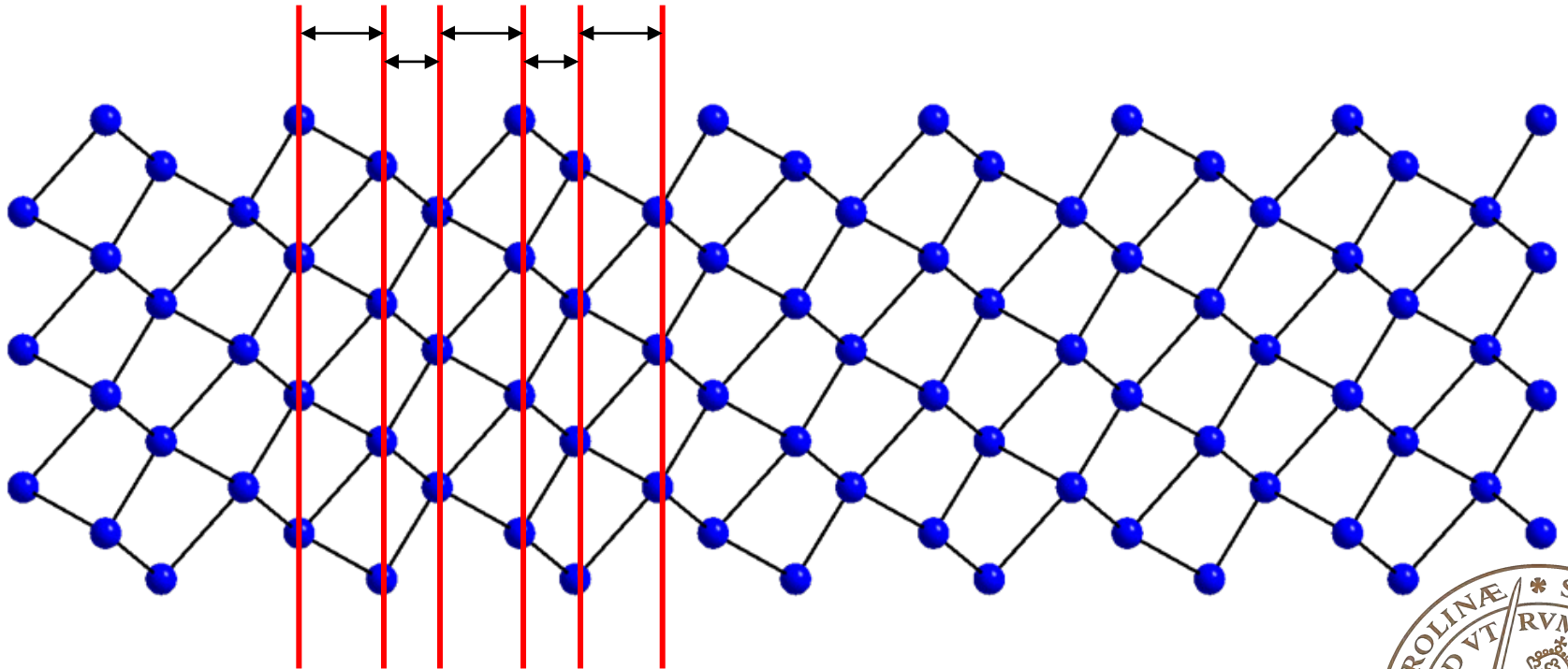
- 1) What is the structure of Stistaite?
- 2) What is all the garbage in Sn-rich Stistaite?





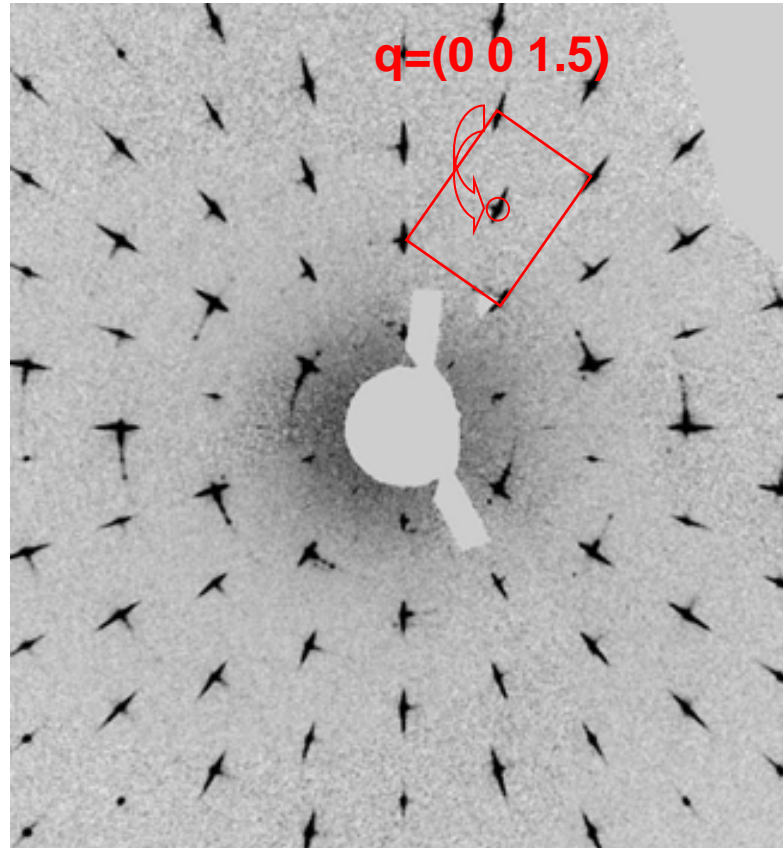
# 1) What is the structure of Stistait?

Das Urstoff Sb! Each Sb is 3-bonded to yield a full octet



# Das Urstoff Sb - diffraction

Sb is a doubled PC structure. The effect is very strong, and it is difficult to distinguish between main reflections and satellites. The effect is purely displacive.



# Symmetry/Cell

$R-3m(00\gamma)00$

Sb :a=4.310 c=5.640 q=(0,0,1.50)

Sb<sub>2</sub>Sn :a=4.329 c=5.412 q=(0,0,1.37)

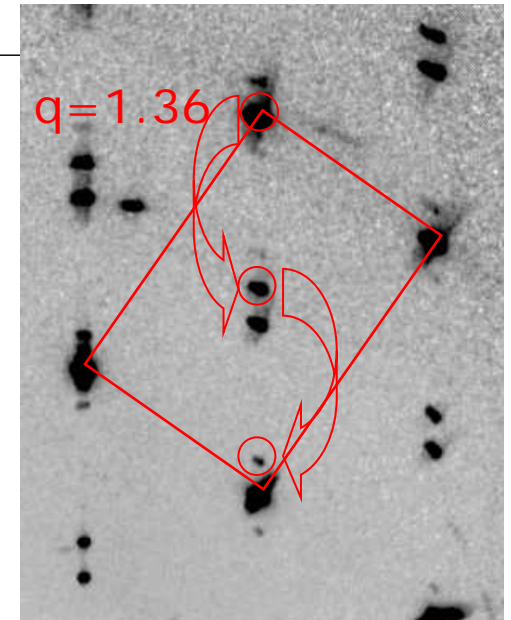
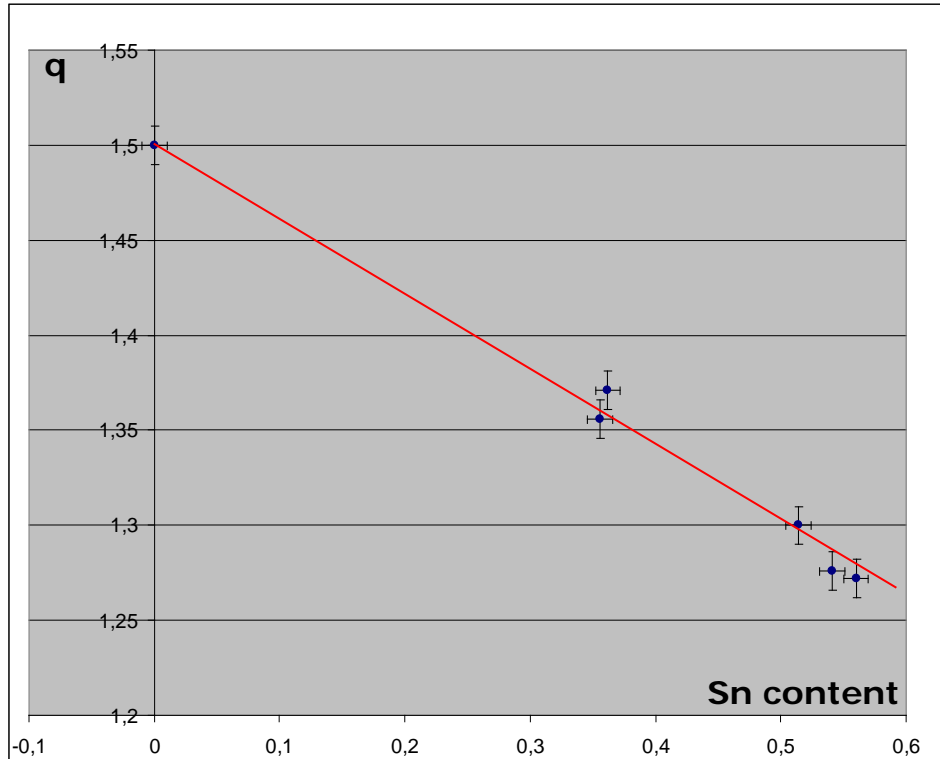
Sb<sub>3</sub>Sn<sub>4</sub>:a=4.340 c=5.312 q=(0,0,1.29)

$$\gamma = 3/2(1 - [\text{Sn}]/4)$$

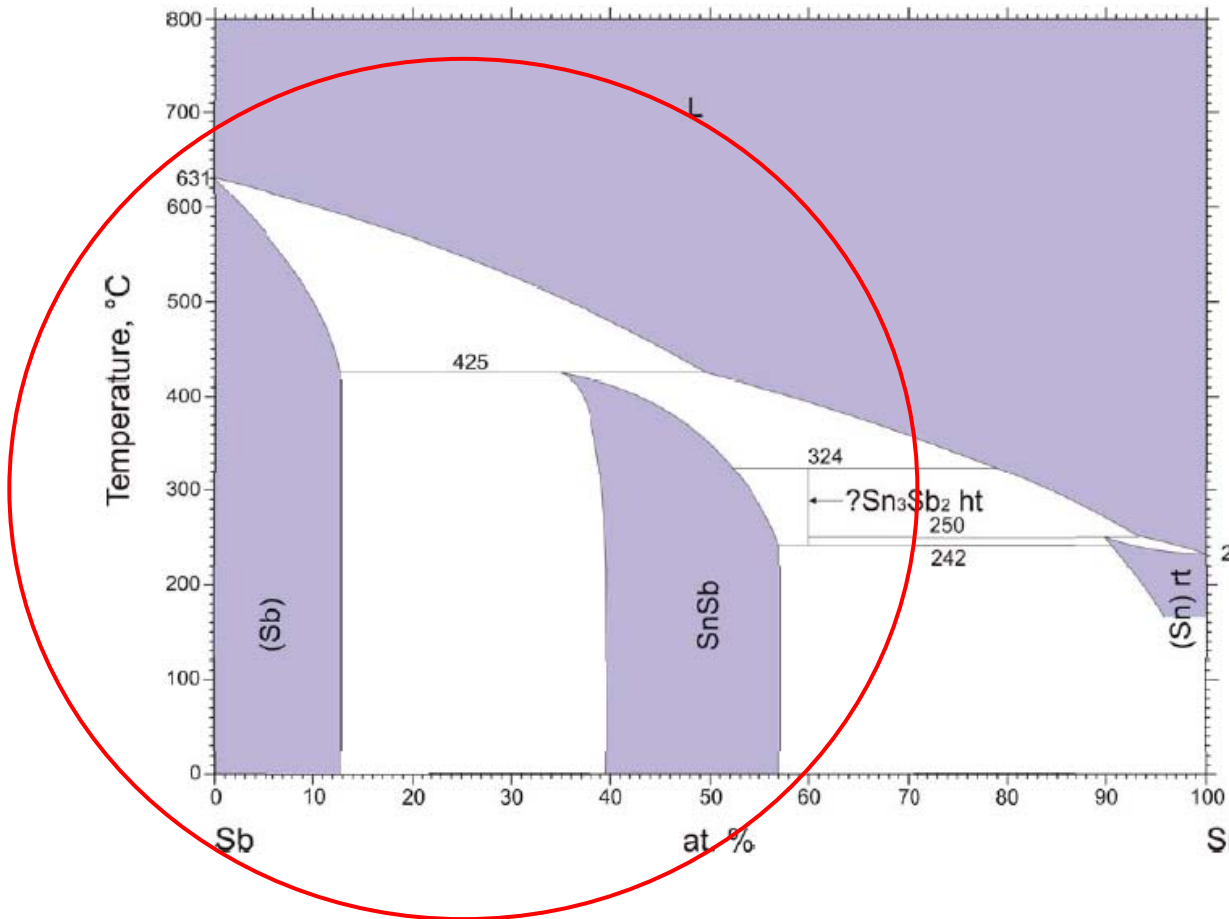
$$[\text{Sn}] = 4(1 - 2\gamma/3)$$



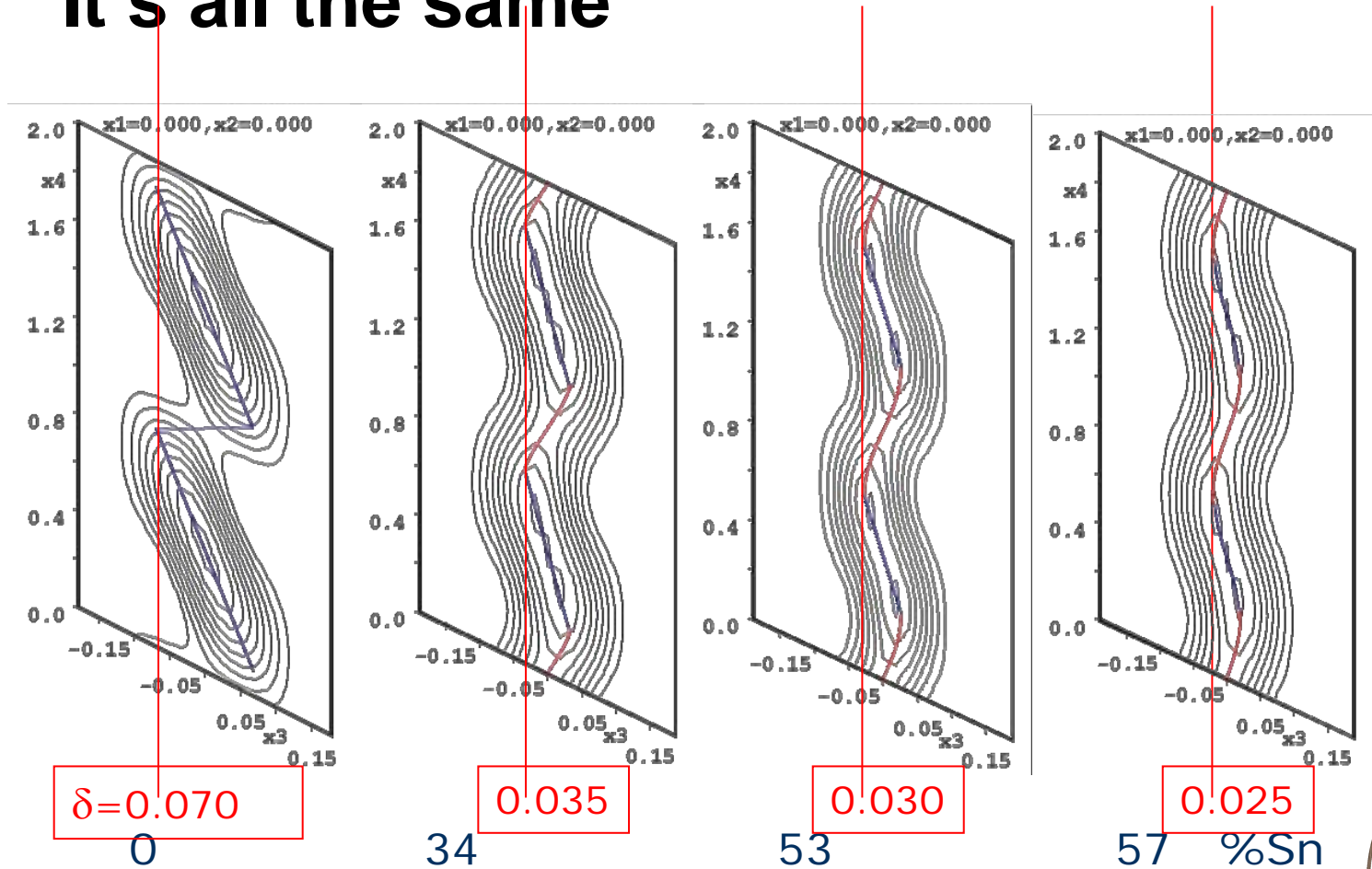
# It's could be all the same



# One discontinuous phase

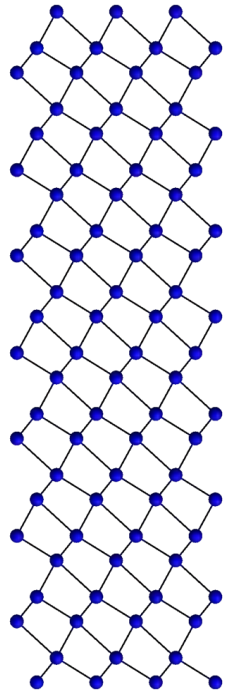


# It's all the same



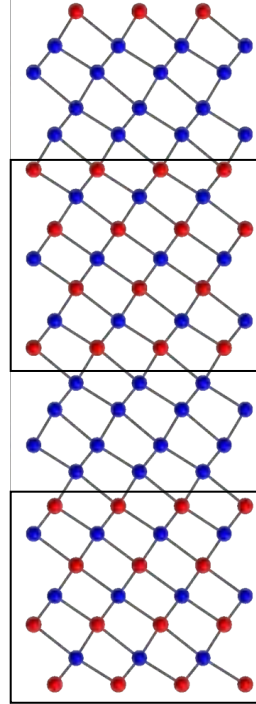


# It's all the same

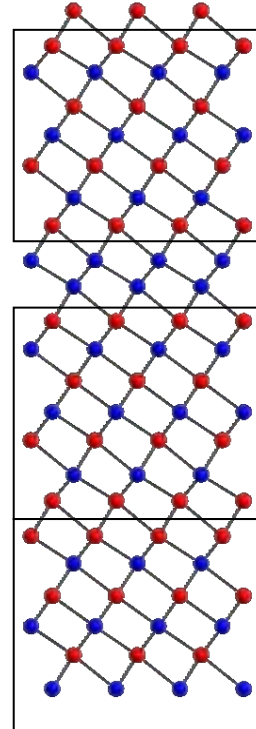


0

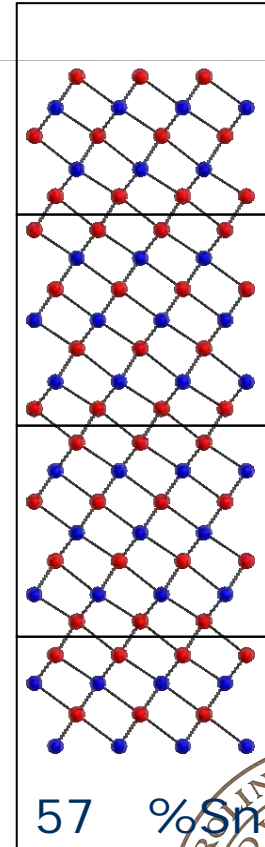
Miscibility gap 13-34%



34



53

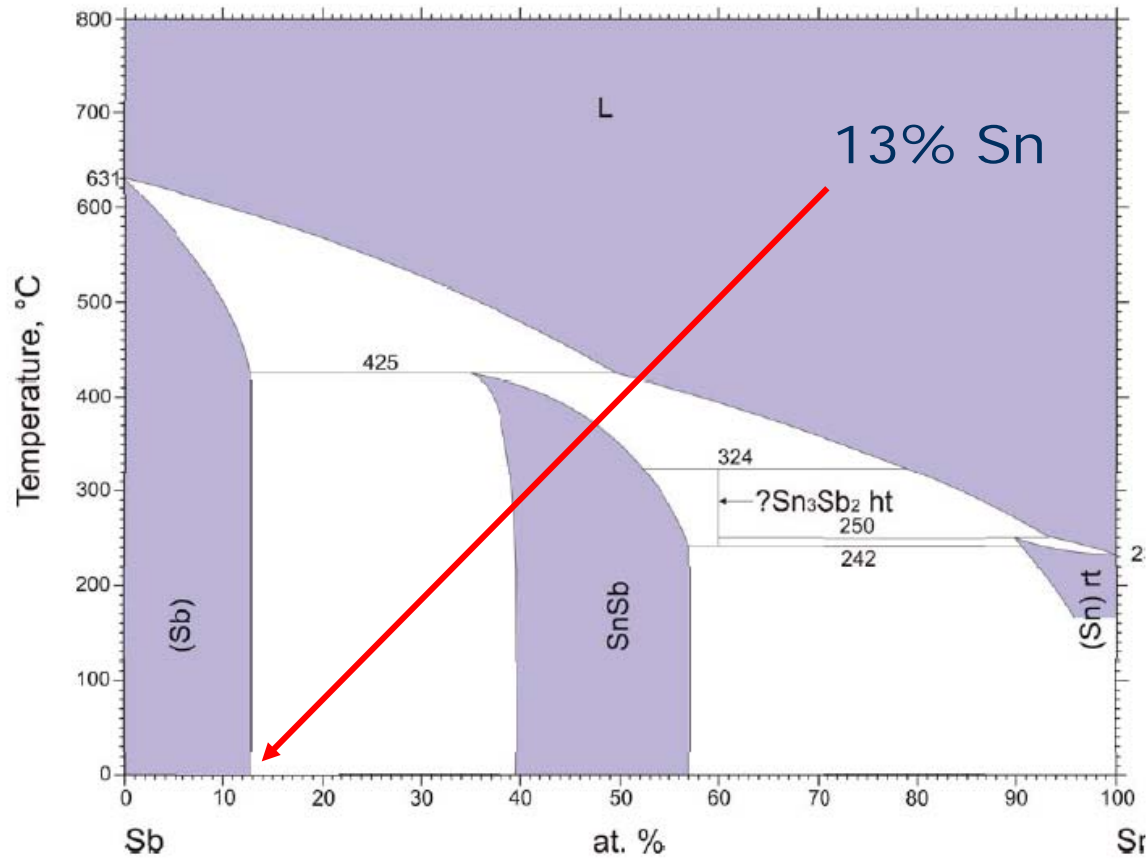


57 %Sn

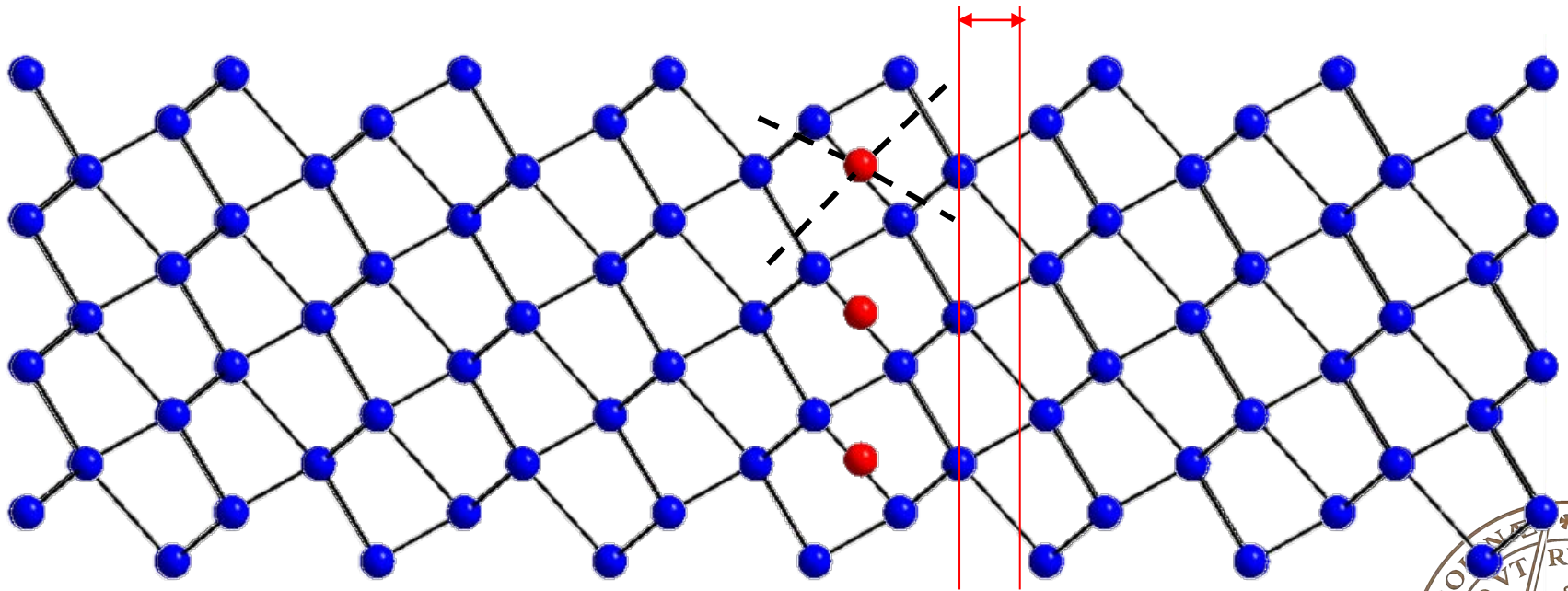




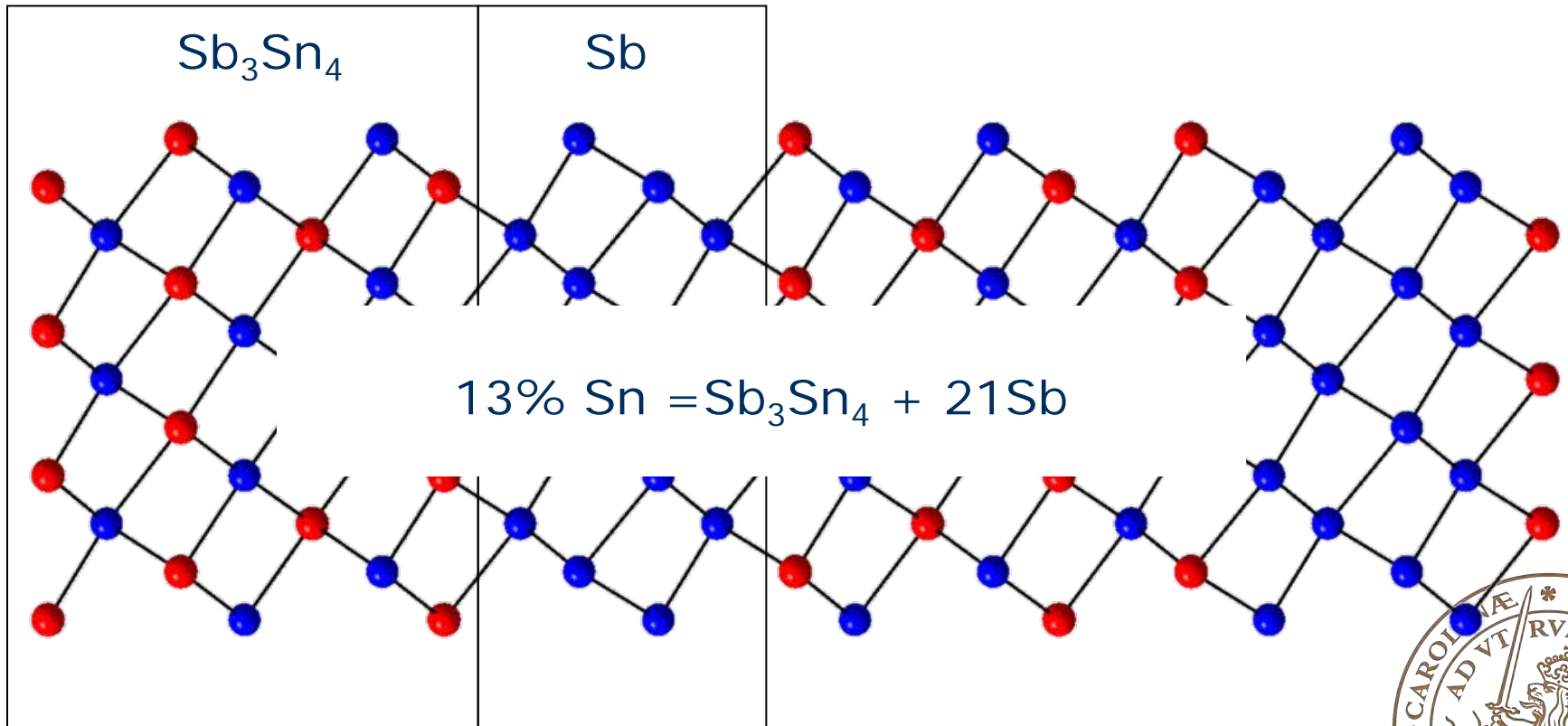
# Solid solution



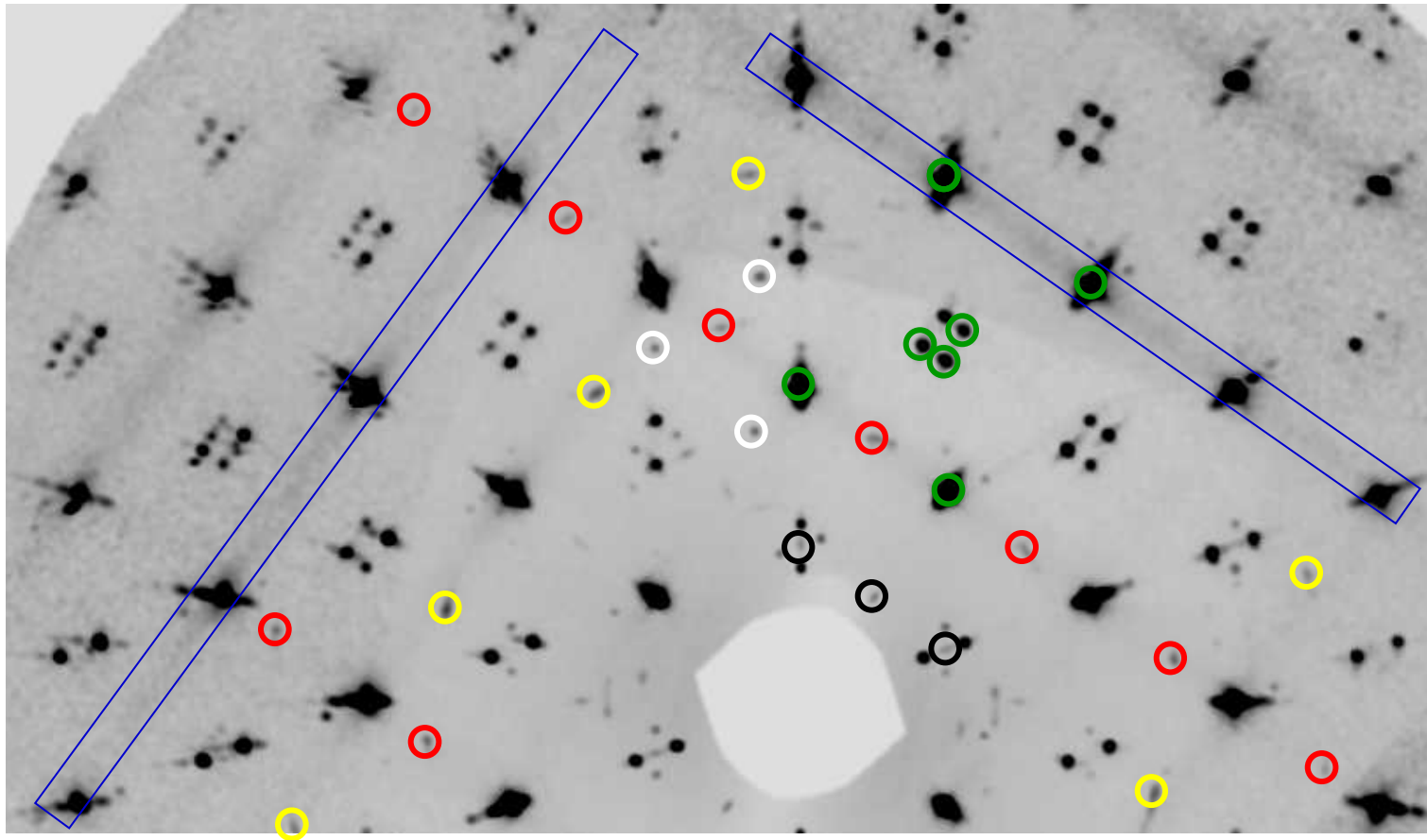
# Solid solution



# Solid solution



## 2) What is all the garbage in Sn-rich Stistaite? Twin'n'Sn!



Stistaite

$\alpha$ -Sn

$\alpha$ -Sn

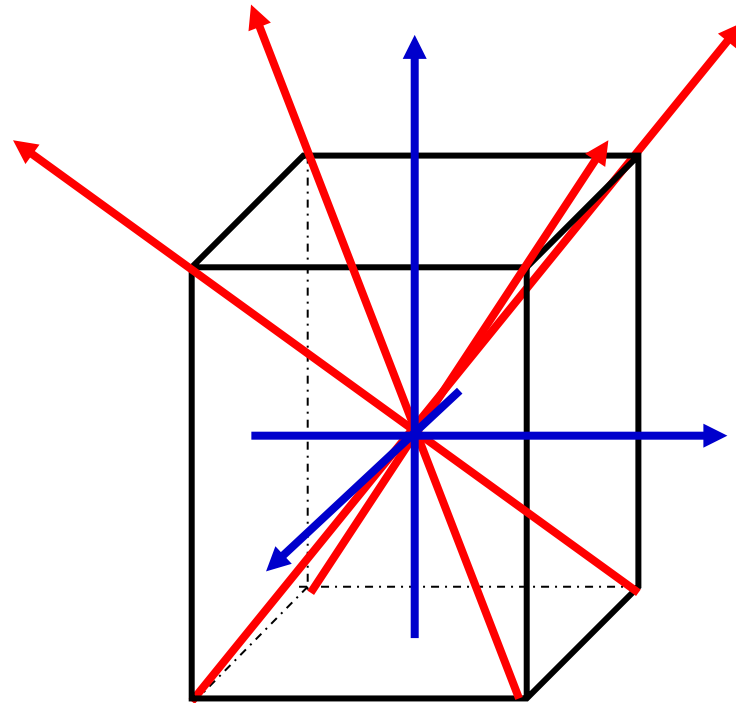
Strain

$\lambda$  half

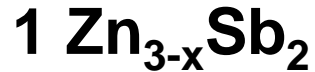


# Composite diffraction pattern

$S_n$  →  
 $S_b S_n$  →



# Examples

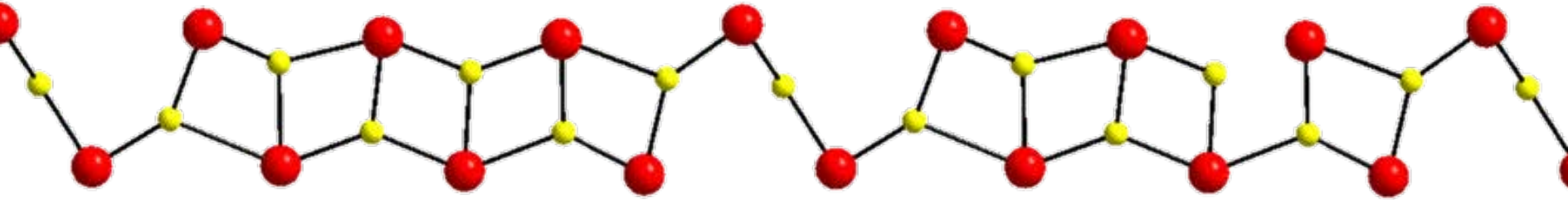


2 Stistaite

3 **Onoratoite**



# Onoratoite

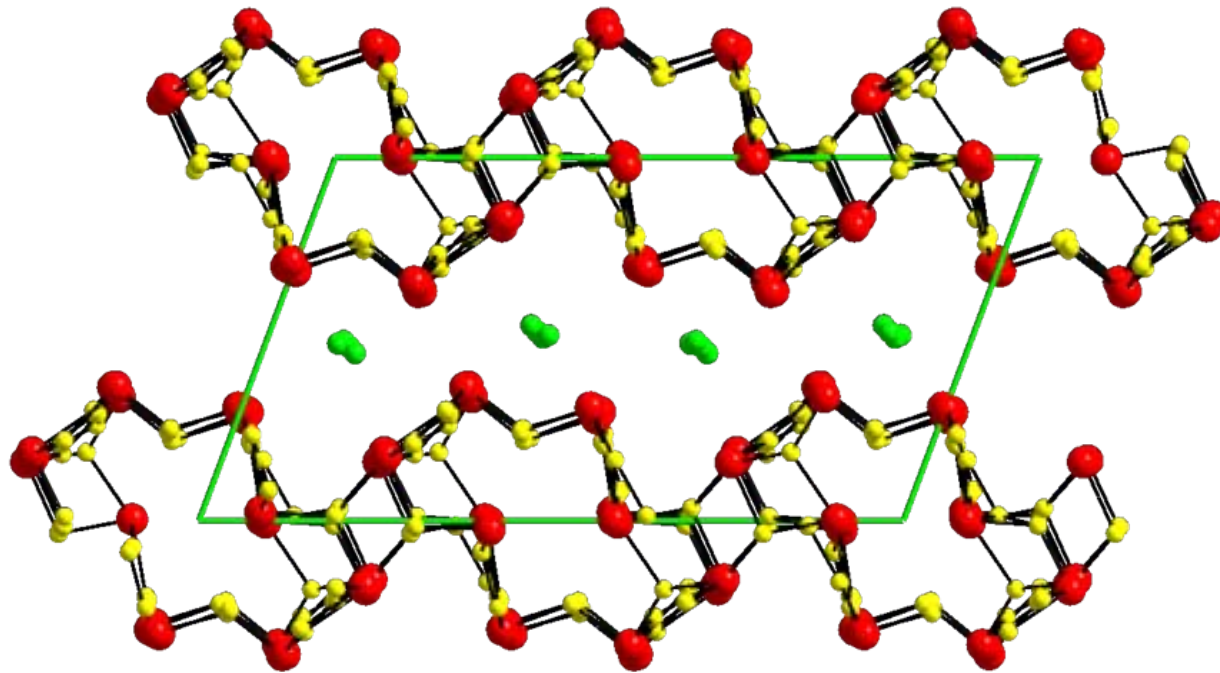


In each column, oxygen vacancies order to form a fourfold superstructure along b.

Cl-onoratoit has  $q = 0 \frac{1}{4} 0$  while for I-onoratoit  $q \approx \frac{1}{2} \frac{1}{4} \frac{1}{6}$



# Onoratoite





# Onoratoite

Strategy for structural solution:

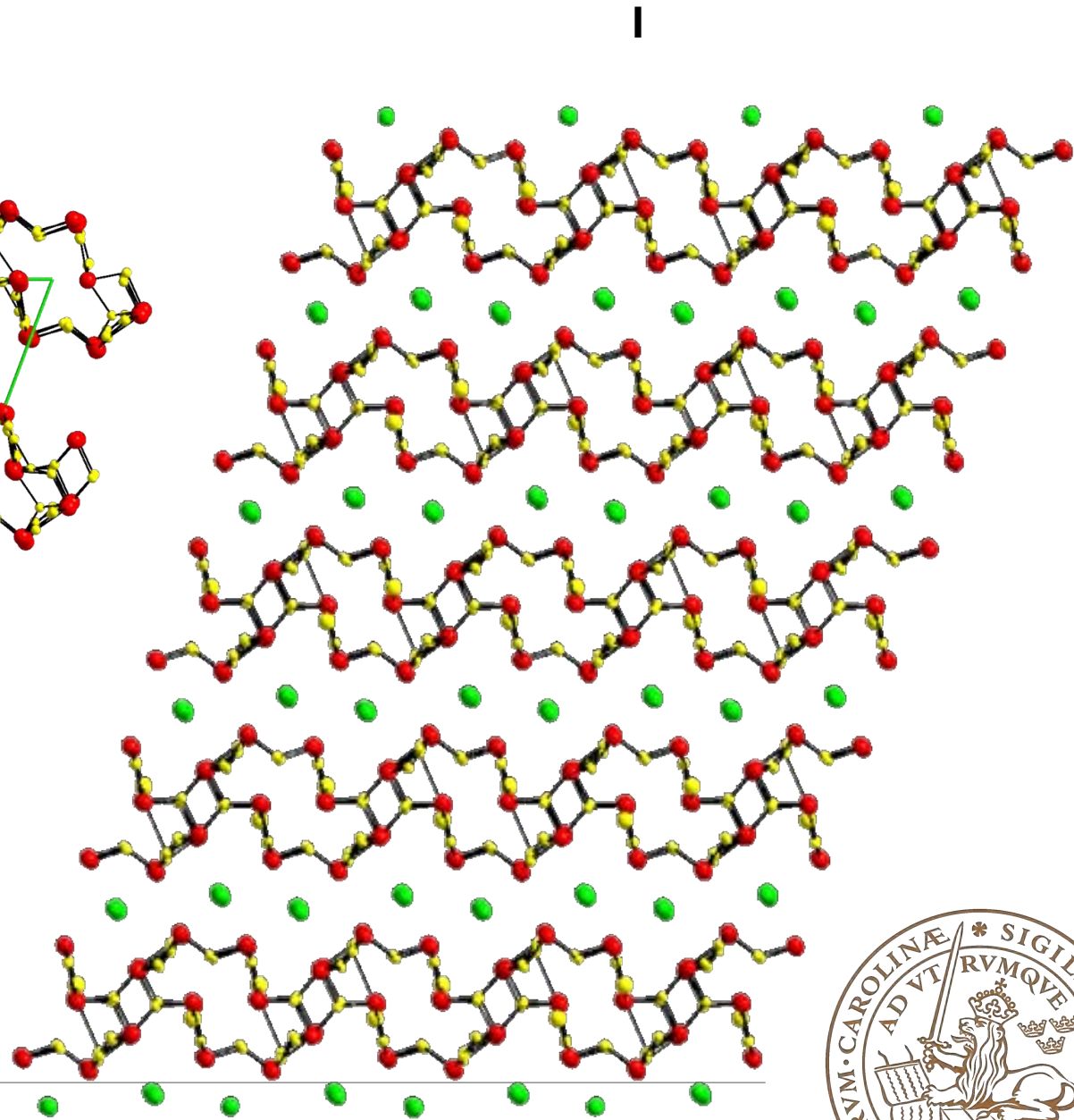
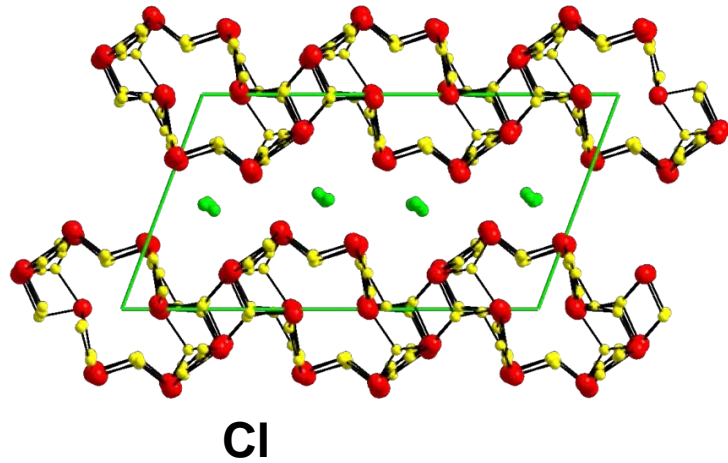
Take super structure from Cl-Onoratoite, convert to modulated structure  $q=(\frac{3}{4} \frac{1}{4} 0)$

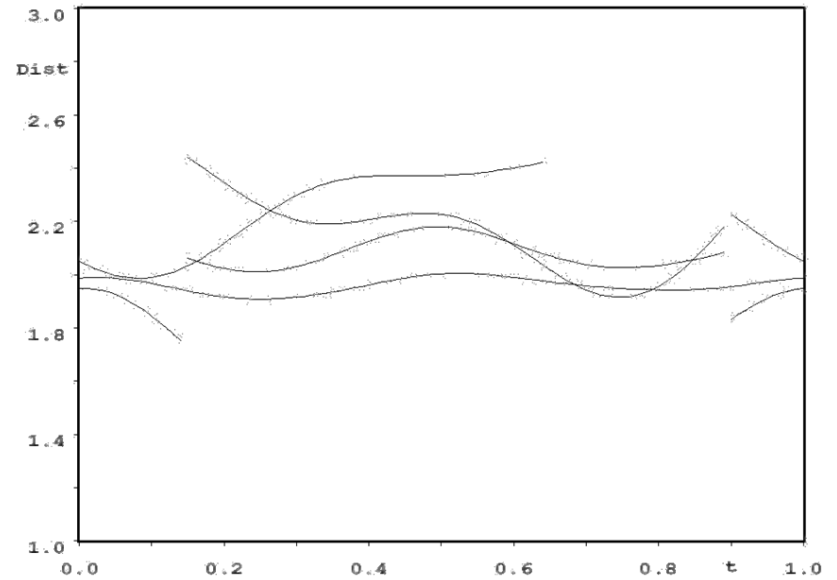
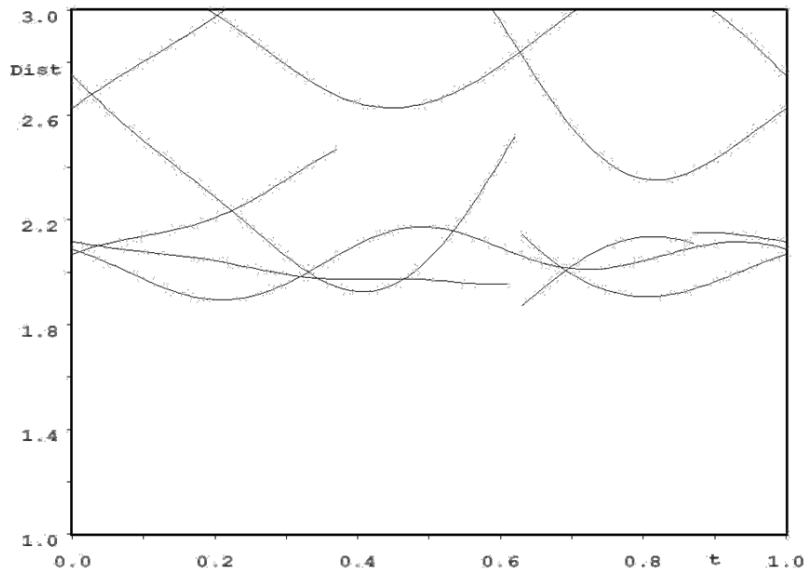
Reduce symmetry to triclinic, use parameters as starting model for I-Onoratoite  $q\approx(0.5 \ 0.25 \ 0.16)$

Refine. Very small change.

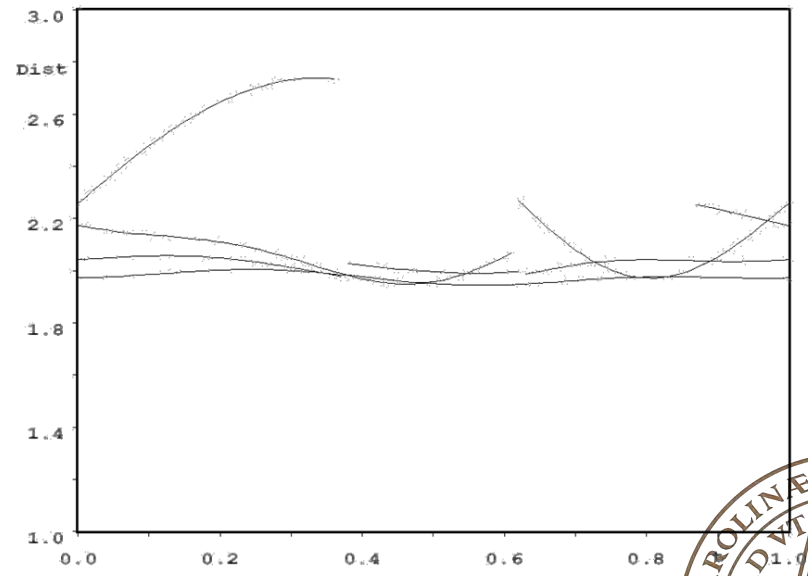
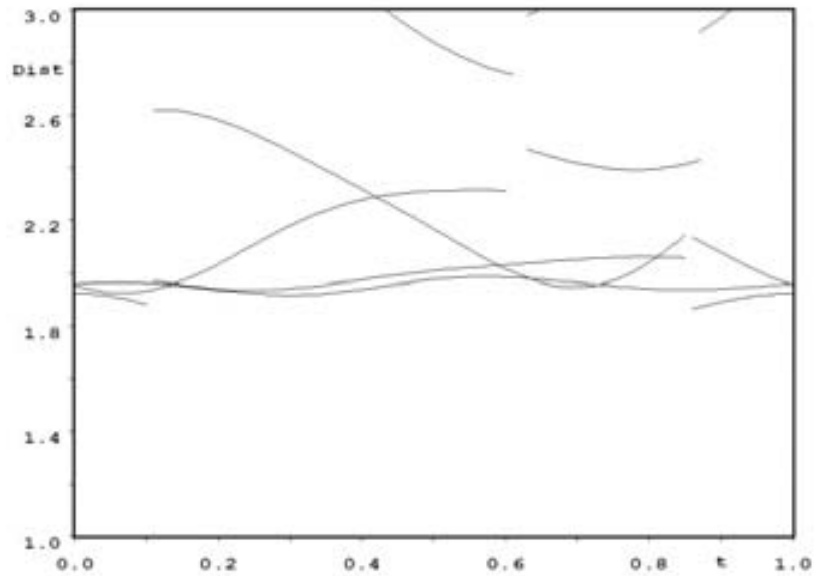


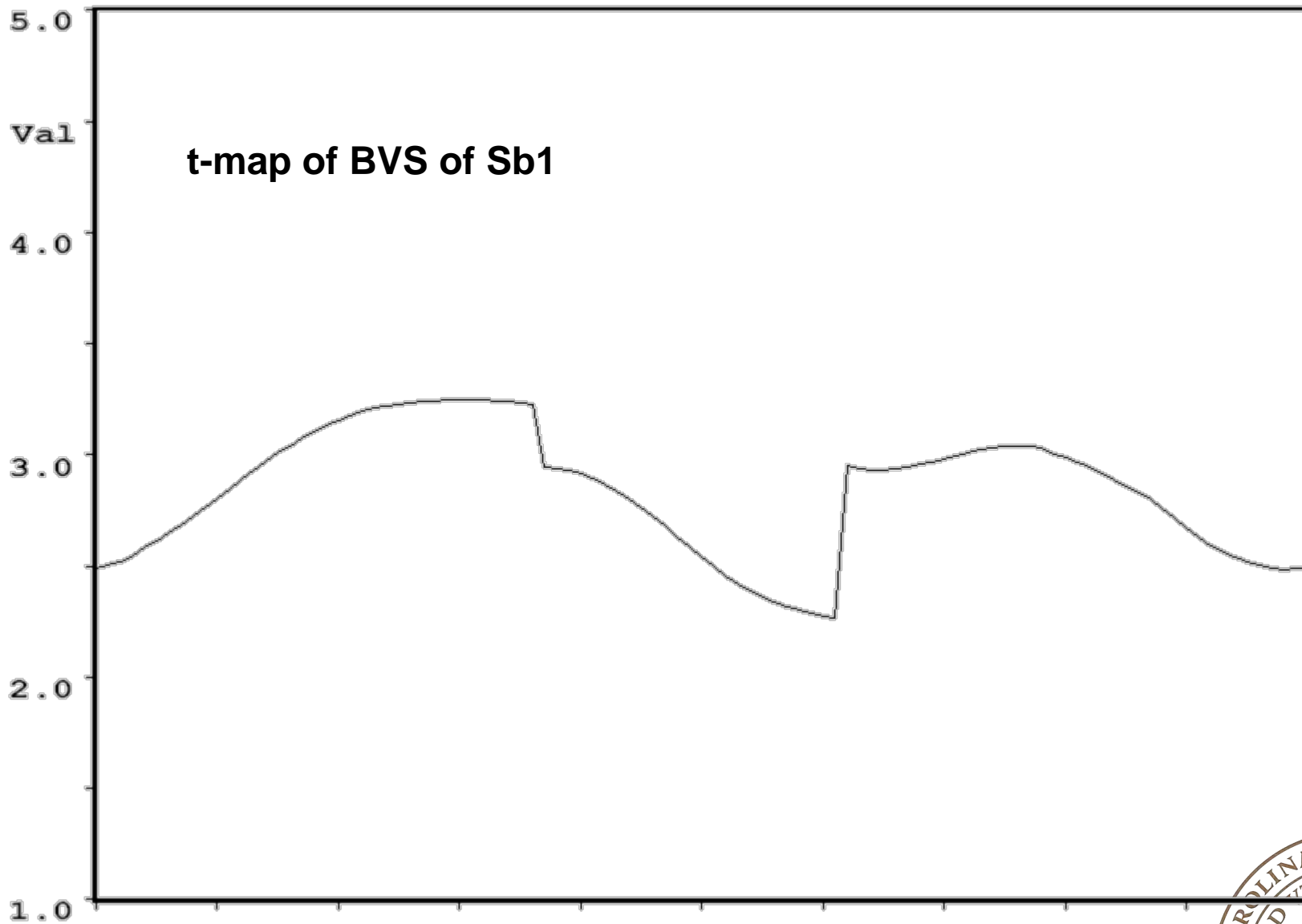
# Onoratoite



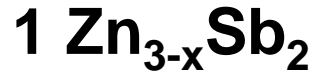


**t-map of Sb-O distances**





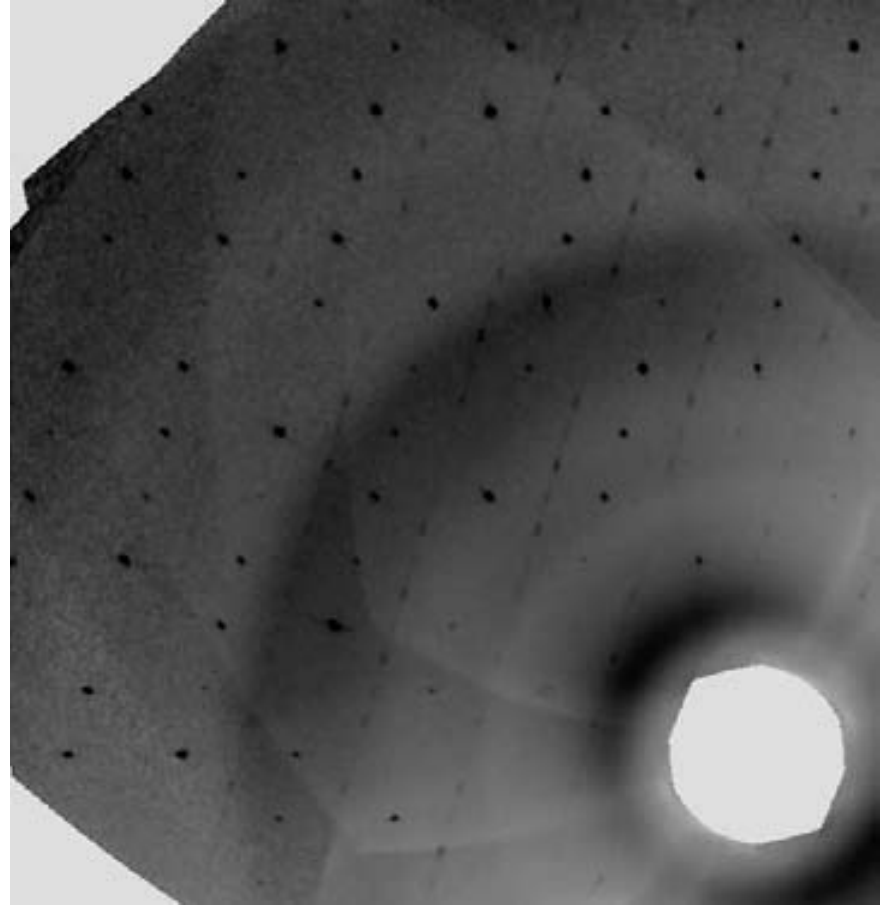
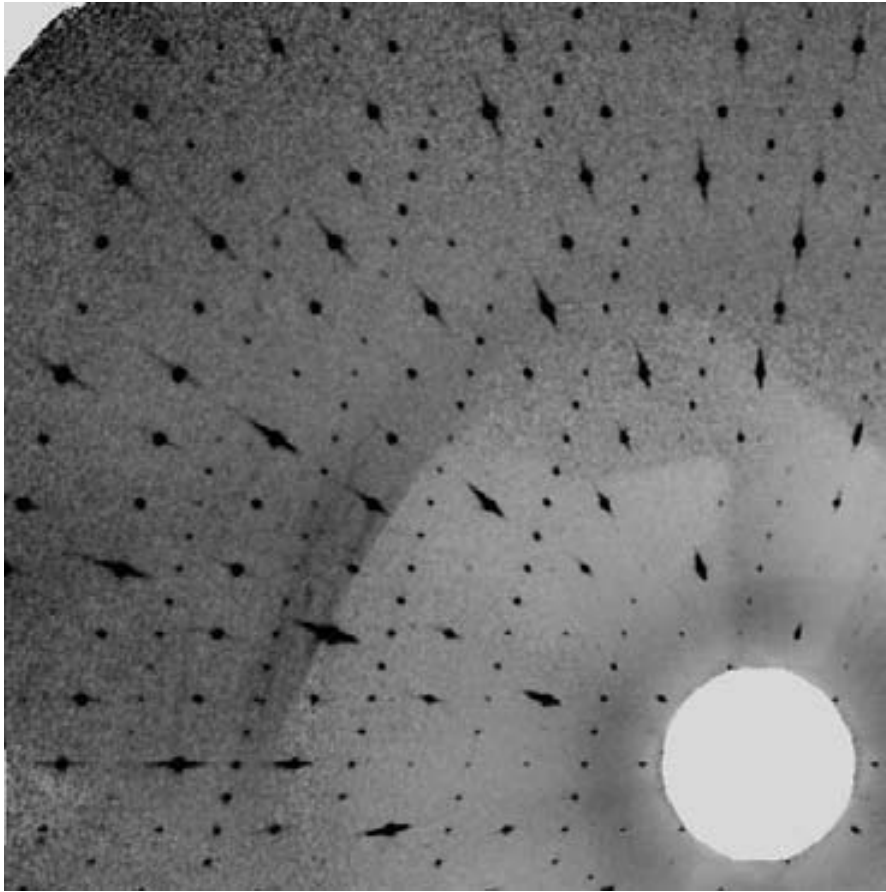
# Examples



2 Stistaite

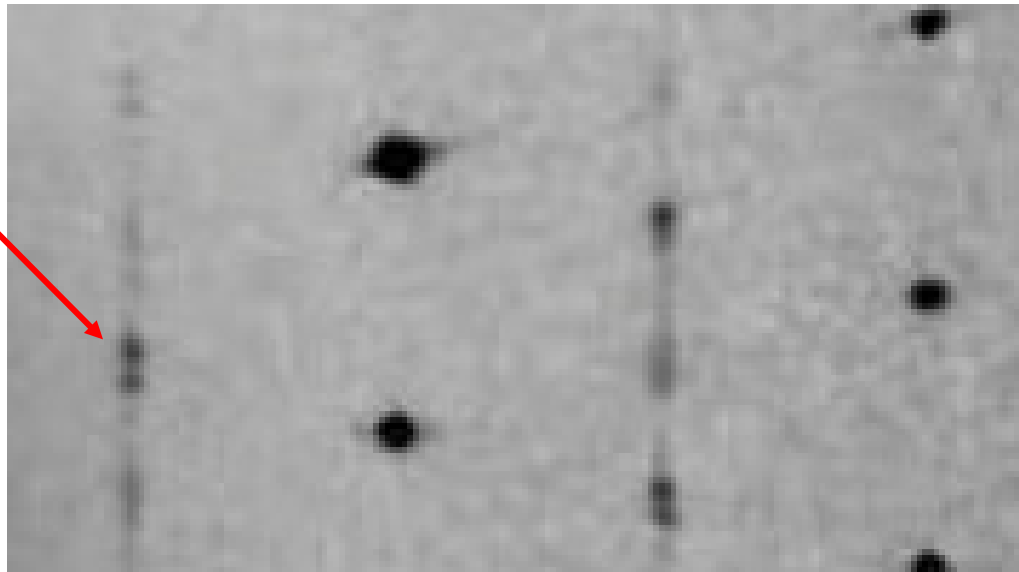
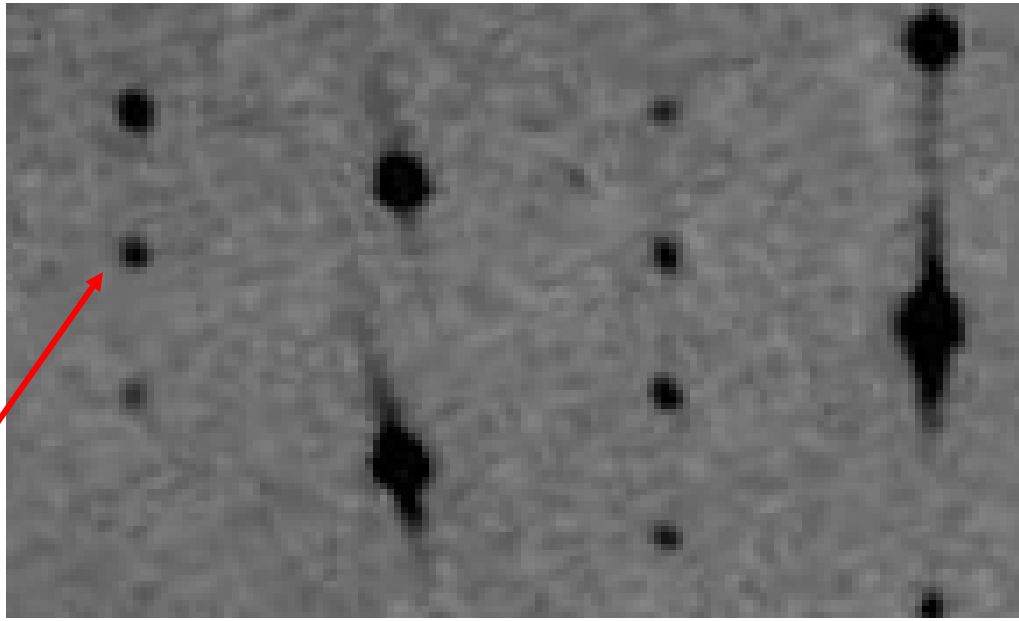
3 Onoratoite





**Projections  $h0l + h1l$ . Normal left. Modulated right**





**Note the  
splitting  
below**

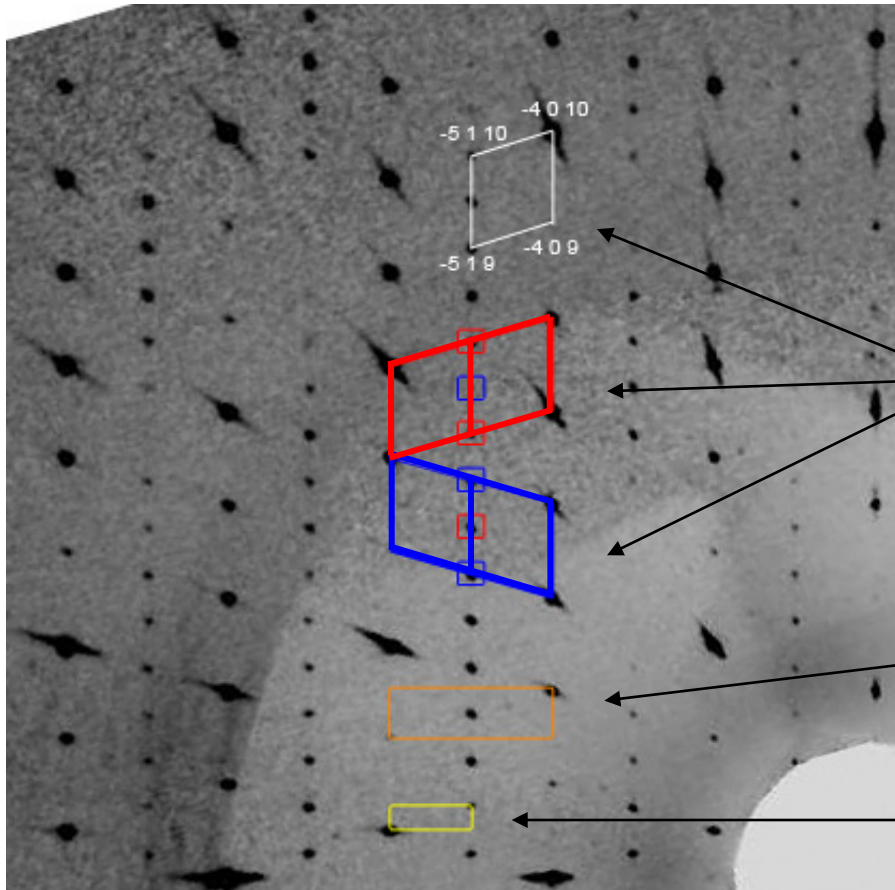


# Interpretation of the pattern for the normal compound

Twinned cell used in refinement,  $C2/m \Rightarrow C-1$

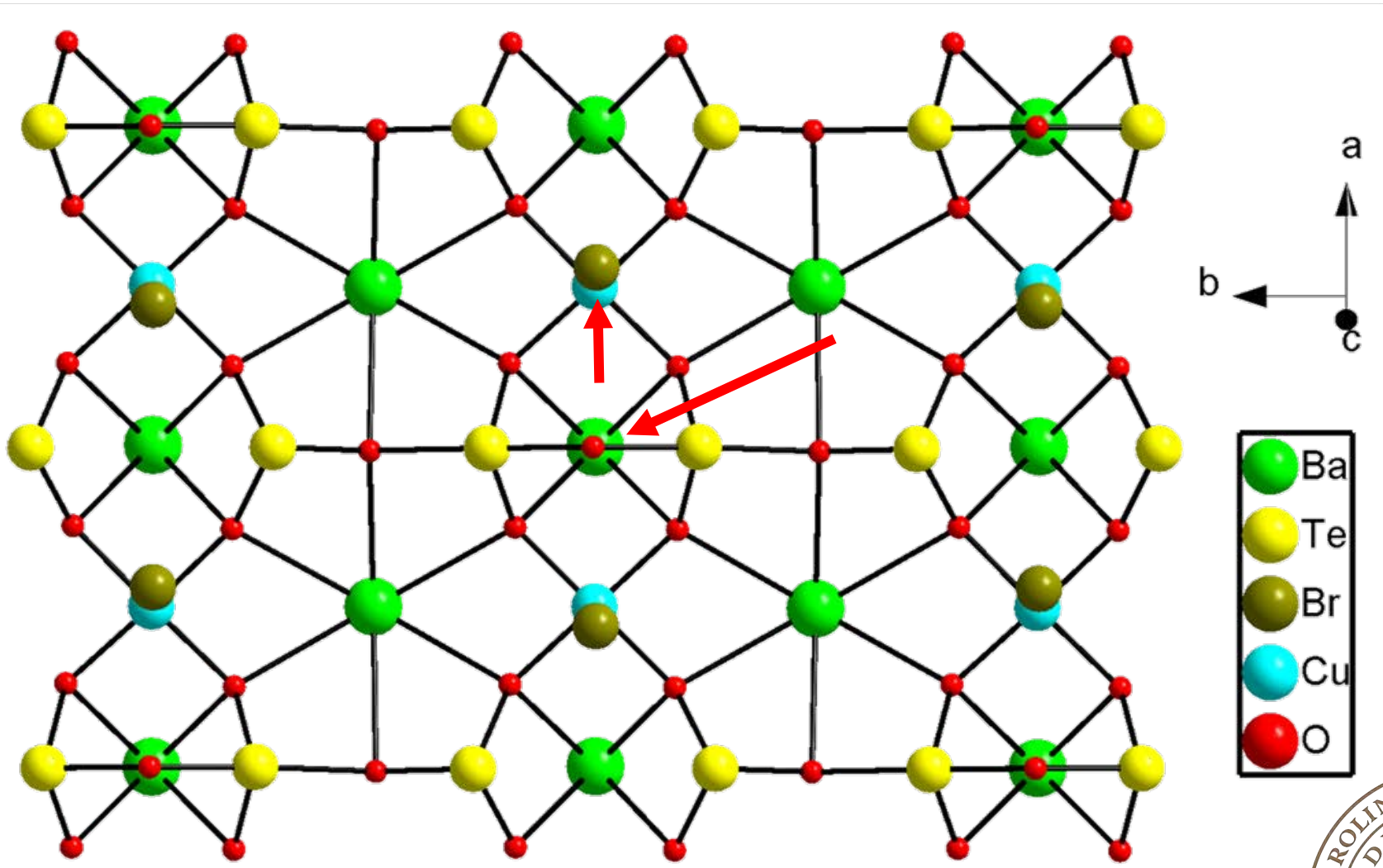
Twin induced superstructure,  $Fdd2$

Fundamental cell,  $Bmmb$





# Cause of super structure – O11- Effect Br



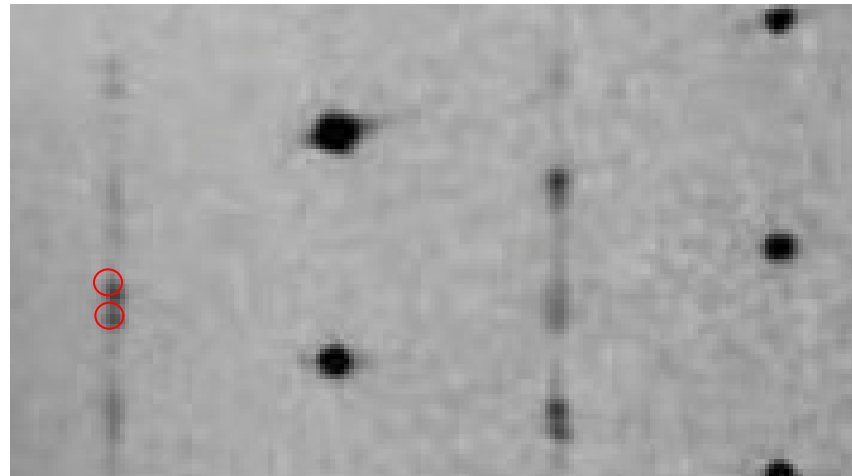
# But...

The compound is (slightly) unstable in air, and a sample left in contact with moisture loses the sharp super structure reflections to diffuse streaks.

A sample sealed under ambient conditions shows an incommensurate modulation,

$$q \approx (0 \ 0 \ 1/16)$$

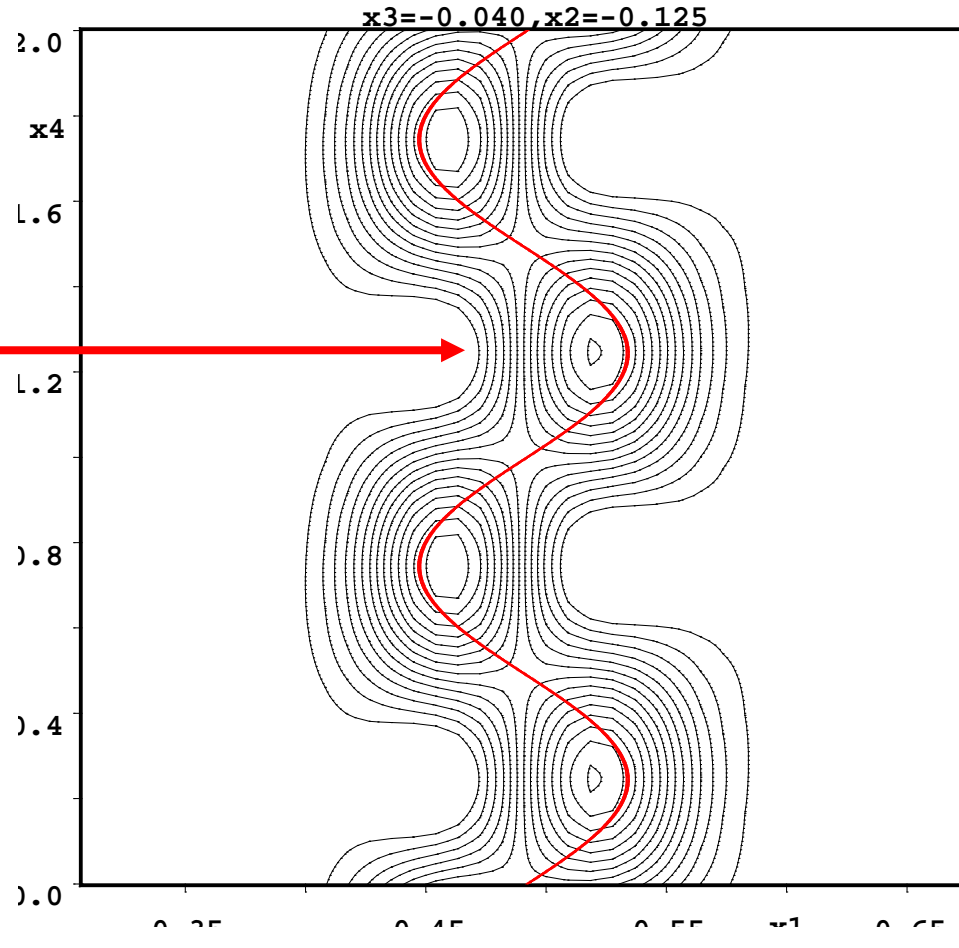
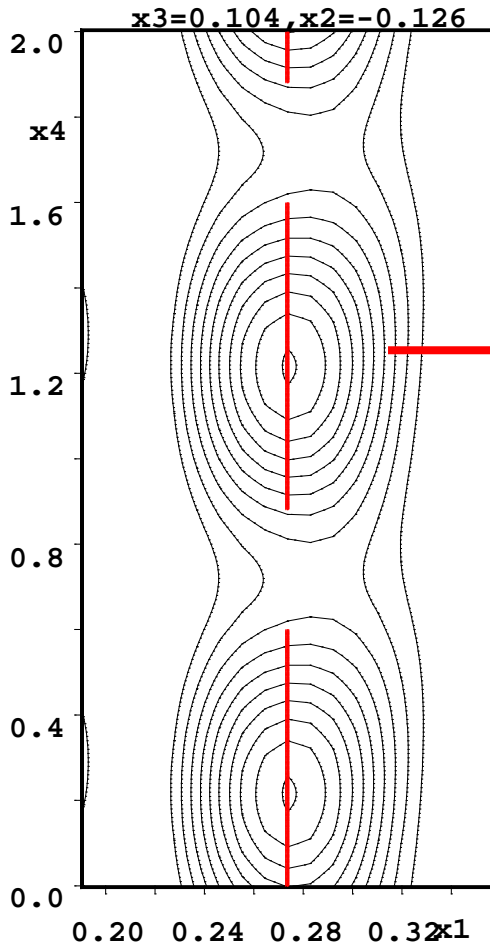
instead of the superstructure reflections.



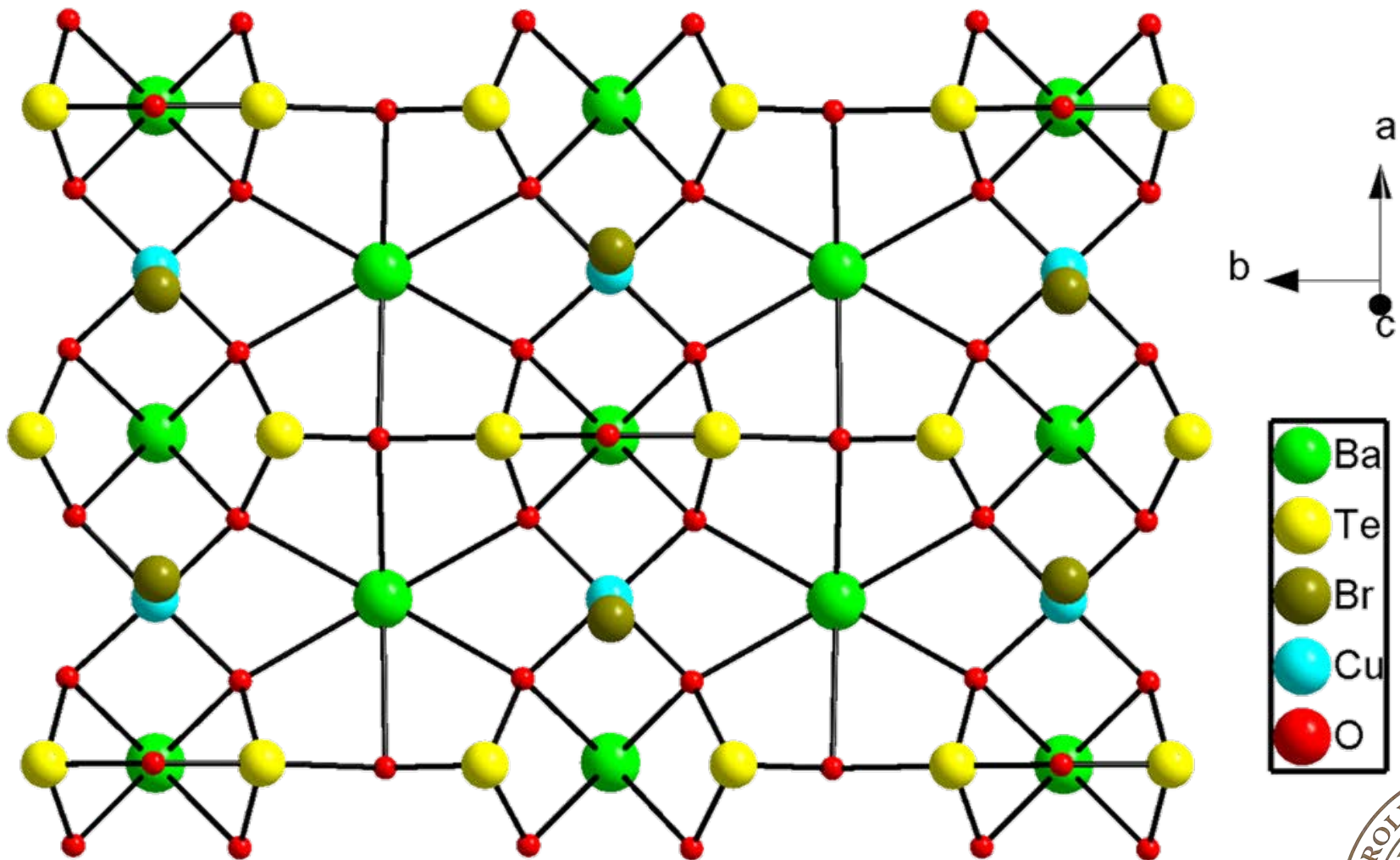
# Modulation

O11

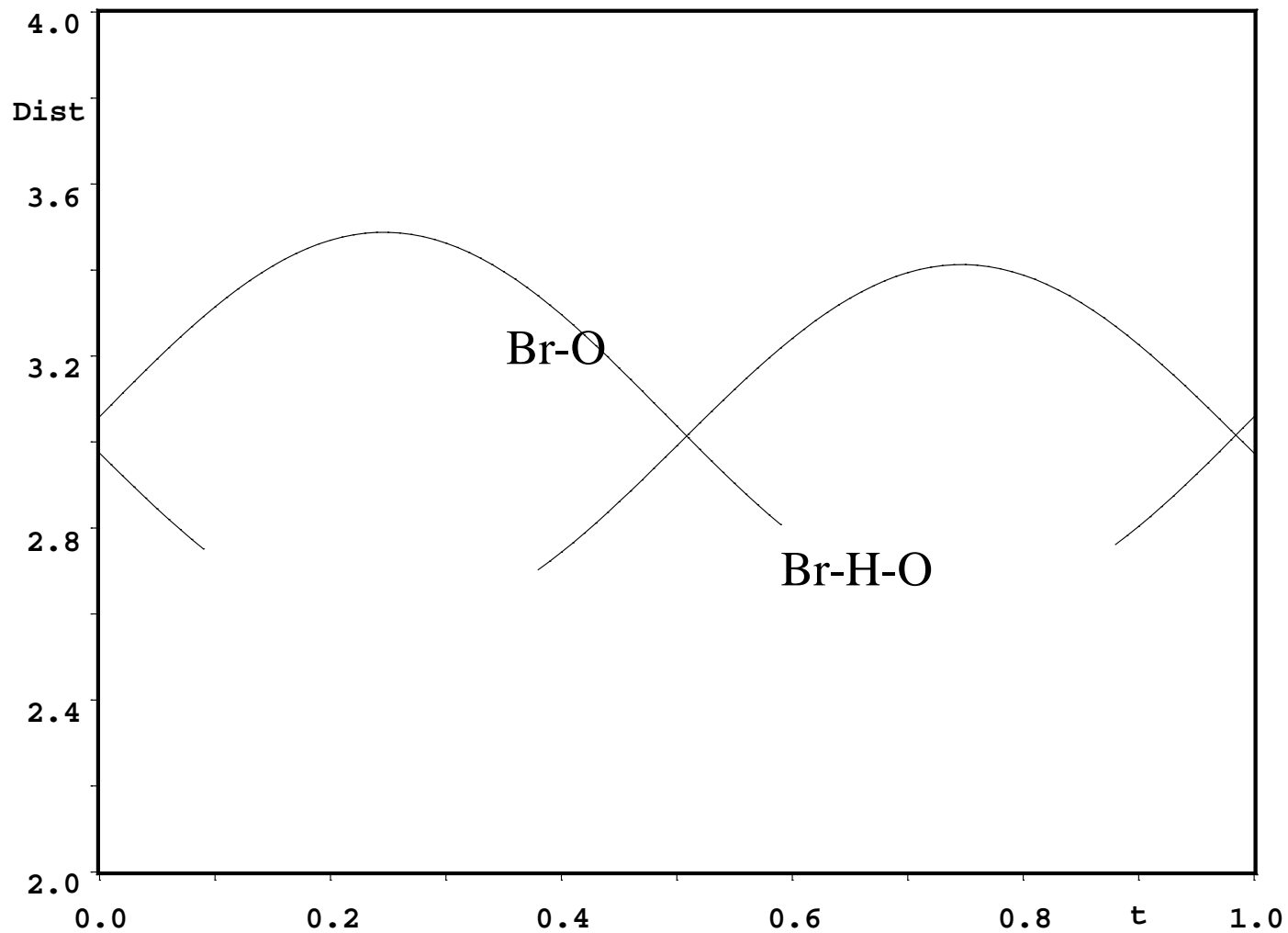
Br



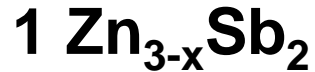
# Exchange of O for OH



# Distances Br-O



# Examples



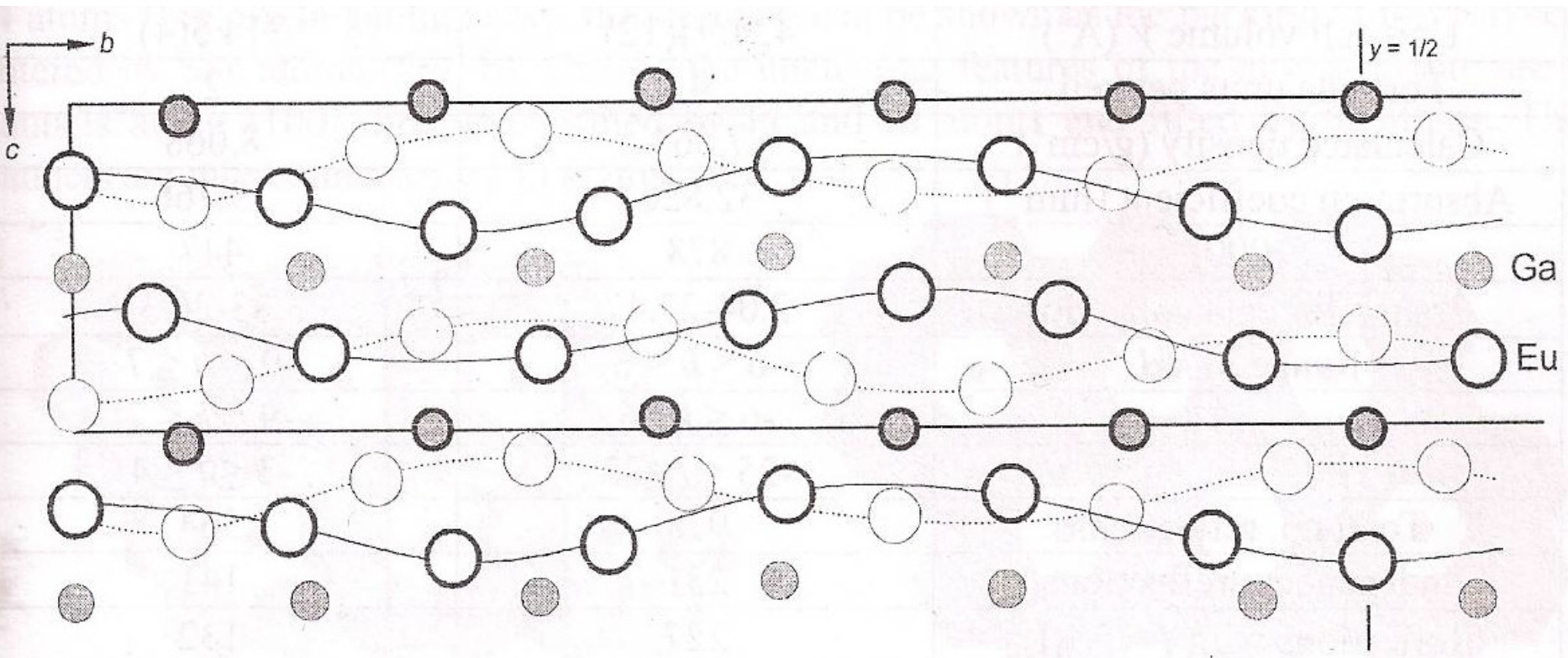
2 Stistaite

3 Onoratoite





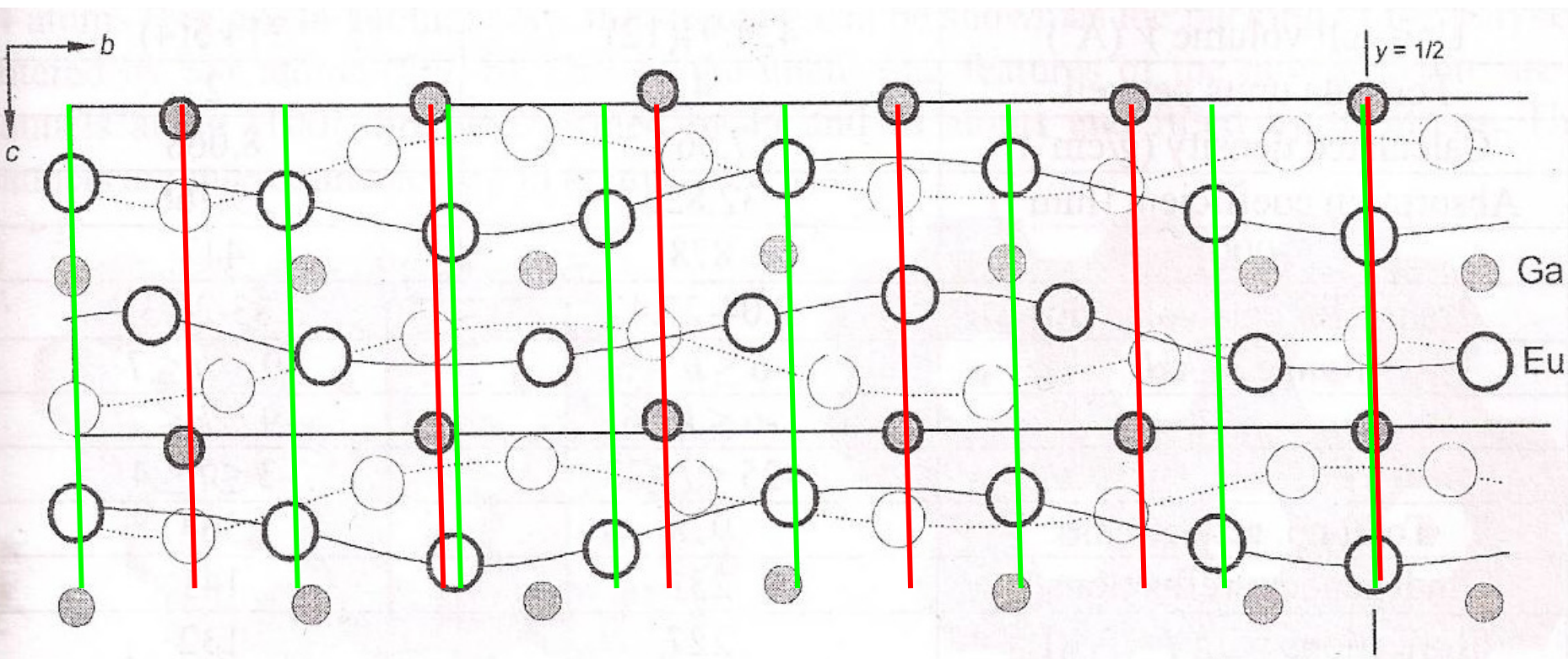
# Memories of Lviv (Lvov, Lwow, Lemberg, Leopoldis)





$Imm2$ ,  $a=5.324\text{\AA}$ ,  $b=61.445\text{\AA}$ ,  $c=7.488\text{\AA}$

15 Ca positions, 6 Ga positions





# Composite?

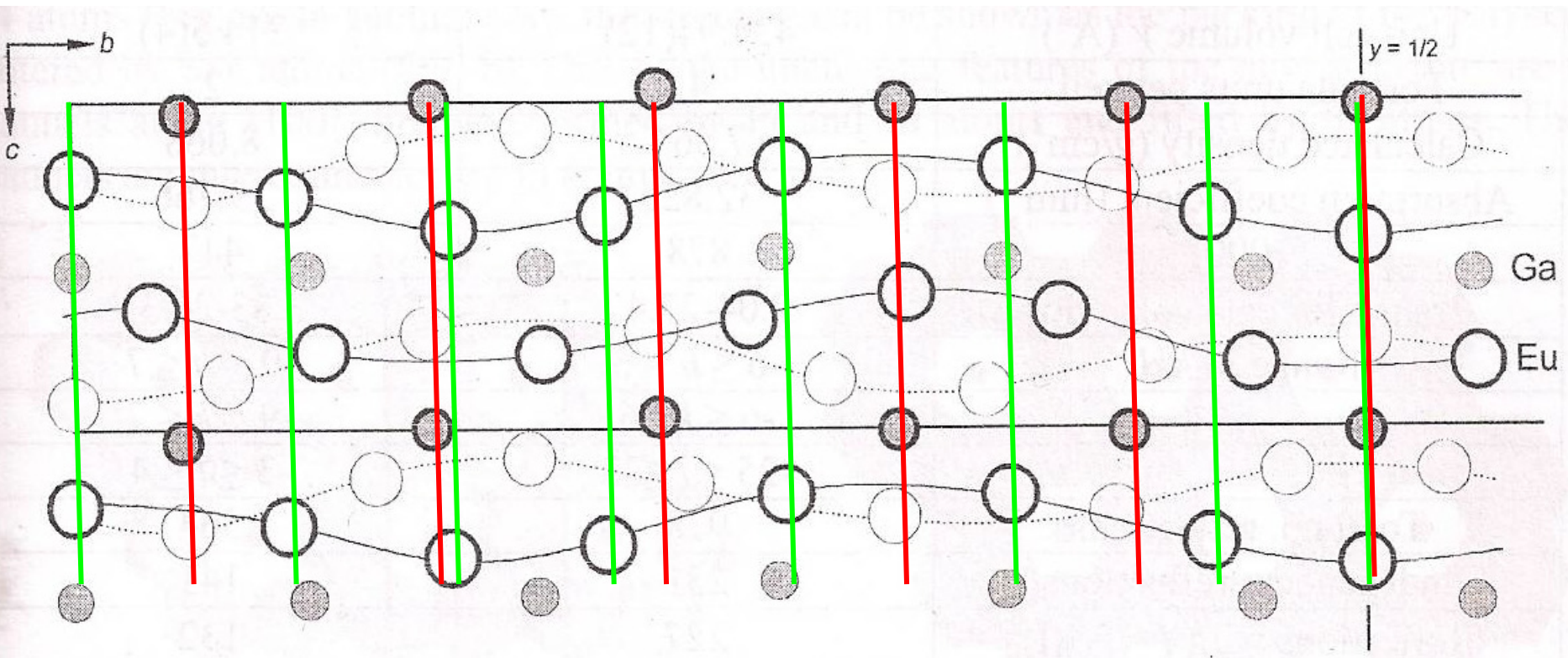
Yes, a single Ga position and one Ca.

$Xmmm(0\beta 0)00s$ ,  $\beta=0.2727=3/11$

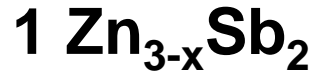
$a=5.324\text{\AA}$ ,  $b=4.7265\text{\AA}$ ,  $c=7.488\text{\AA}$ ,

38 parameters (60)

$\text{Ca}_{28}(\text{Ga,Ge})_{11-x}$  ?



# Examples



2 Stistaite

3 Onoratoite



# Hexagonal Approximants in the $\text{Re}_{13}(\text{Cd/Zn})_{\sim 58}$ Systems



**The Good, The Bad and  
the Ugly**



# CeCd<sub>~4.5</sub>



692 RAYMOND B. ROOF, JR., AND GUY R. B. ELLIOTT

*Inorganic Chemistry*

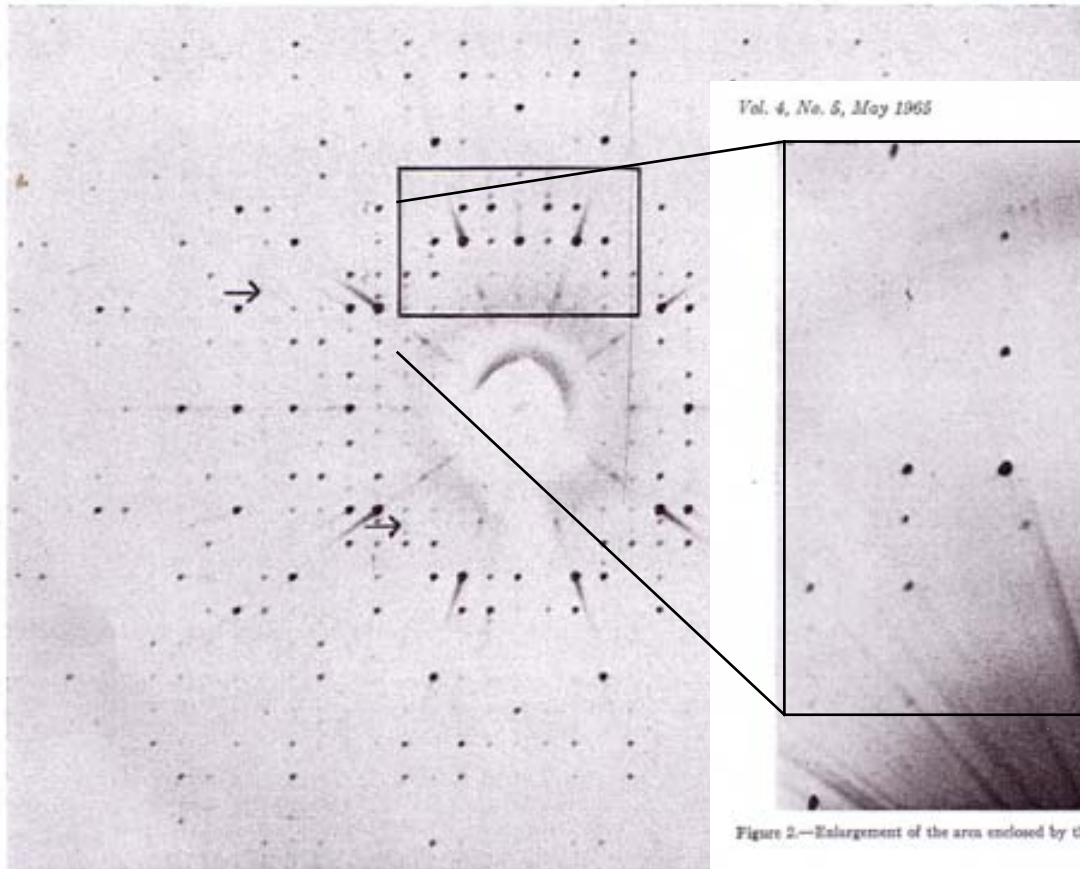


Figure 1.—Superlattice spots on an  $h0l$  view of the parent lattice for a crystal of  $\text{CeCd}_{4.5}$ ;  $\text{Mo K}\alpha$  radiation.

Vol. 4, No. 5, May 1965

MICROPHASES IN  $\text{CeCd}_{4.5}$  SOLID SOLUTIONS 693

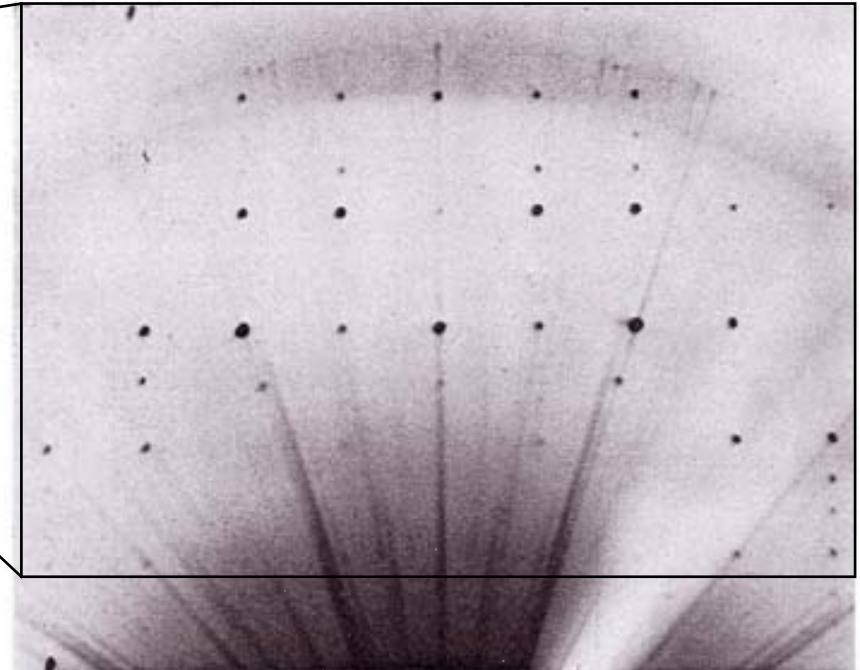
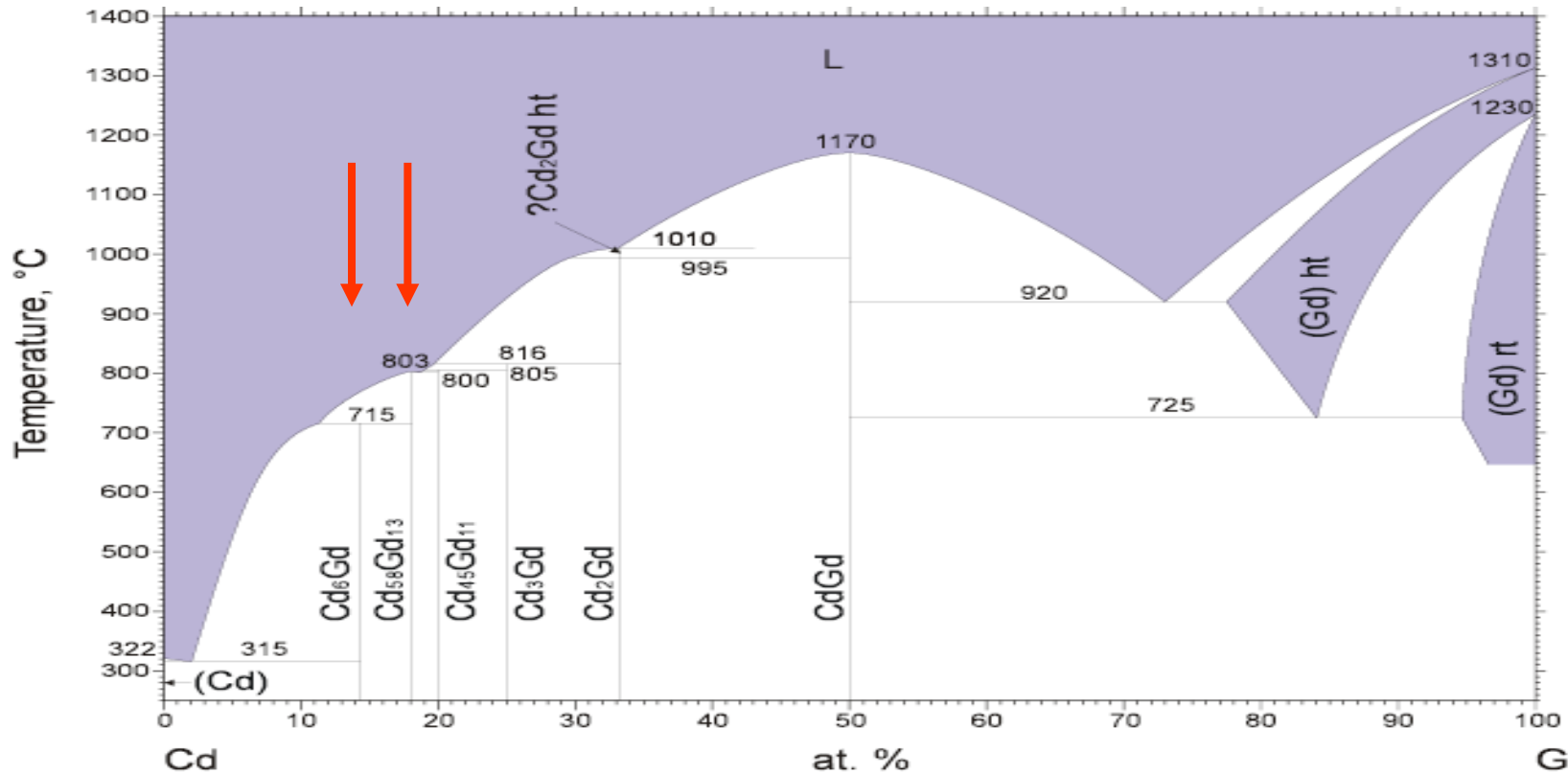


Figure 2.—Enlargement of the area enclosed by the rectangle in Figure 1;  $\text{Cu K}\alpha$  radiation.  $\text{CeCd}_{4.5}$  ( $1/2, 1/2$ ) key pattern, on  $h0l$  view.



# Typical Constitution Diagram



# Hexagonal structures Zn

## Note:

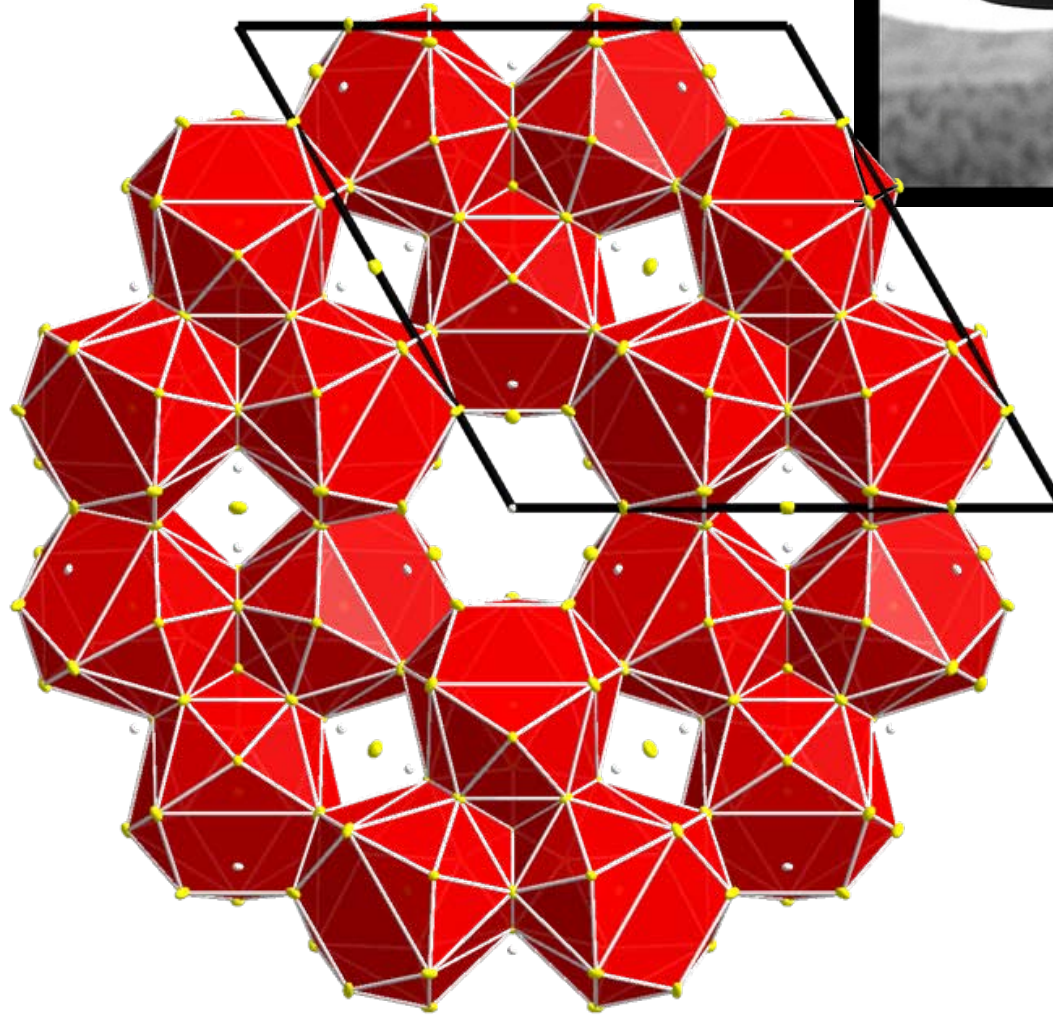
**S.G. determination from satellites, absences and/or failure to refine**

RE	Radius	S.G
Eu	204	-----
Yb	194	P6 <sub>3</sub> /mmc (+ Pc)
La	188	?
Pr	183	P6 <sub>3</sub> /mmc
Ce	182.5	P6 <sub>3</sub> /mmc
Nd	182	P6 <sub>3</sub> /mmc
Pm 181	?????	
Y	181	?
Sm 180	P6 <sub>3</sub> /mmc	
Gd	180	P6 <sub>3</sub> /mmc + P2 <sub>1</sub>
Tb	178	P6 <sub>3</sub> mc + P2 <sub>1</sub>
Dy	177	Pnma
Ho	177	Pnma + Inc
Er	176	Pc2 <sub>1</sub> n
Tm	175	Pc2 <sub>1</sub> n
Lu	173	Pc2 <sub>1</sub> n

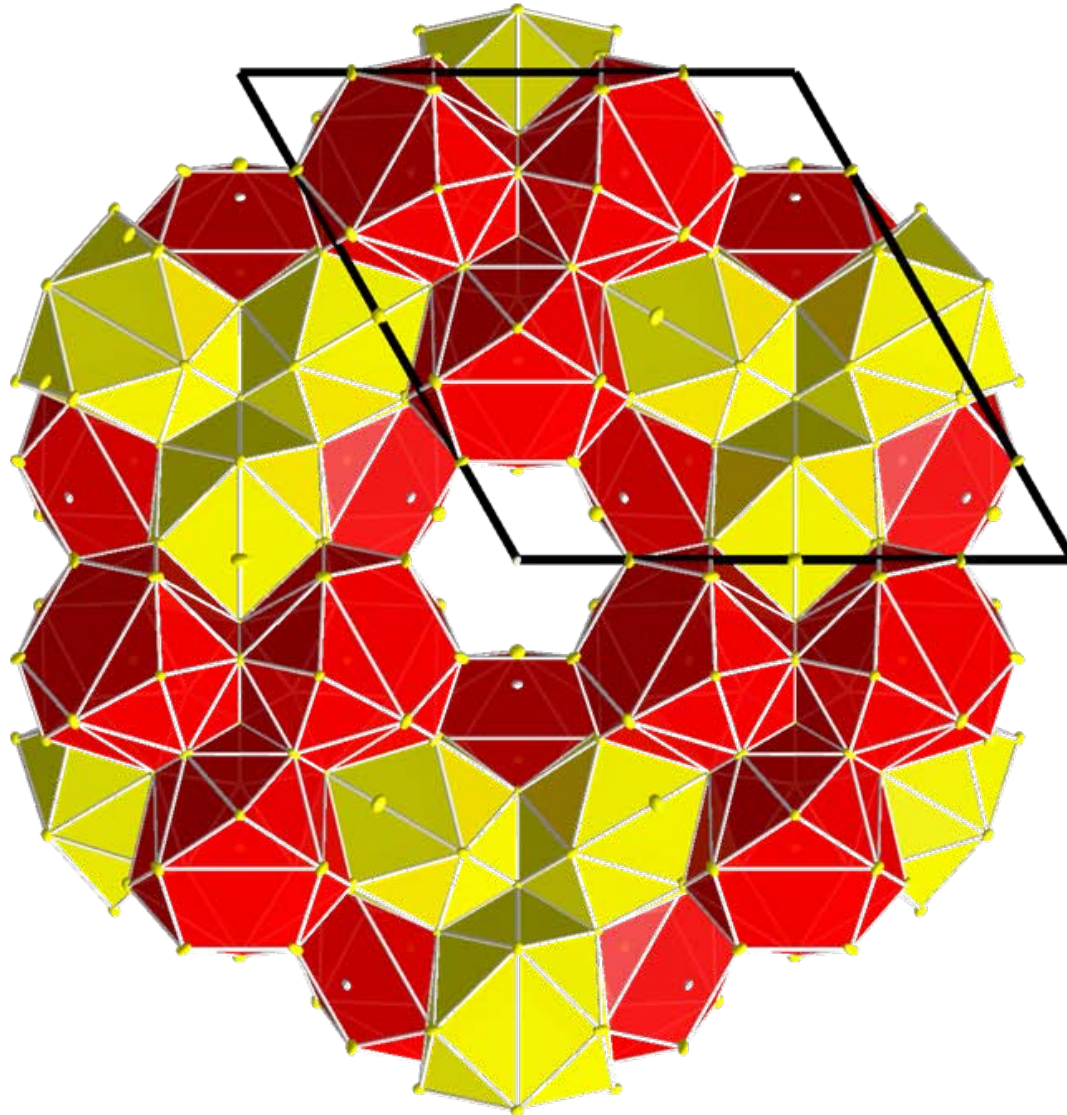




# Complex basic structure

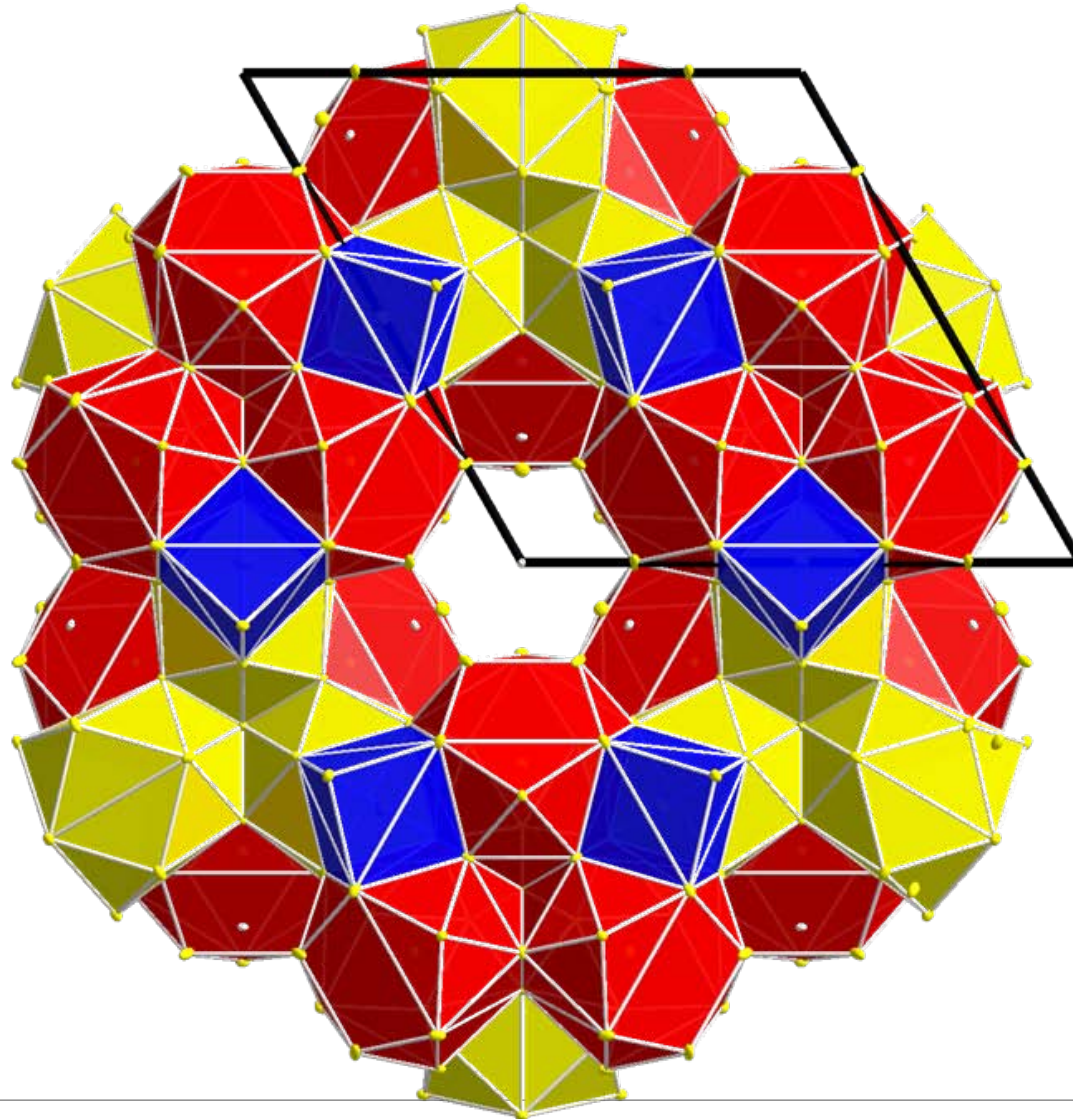


# Complex basic structure

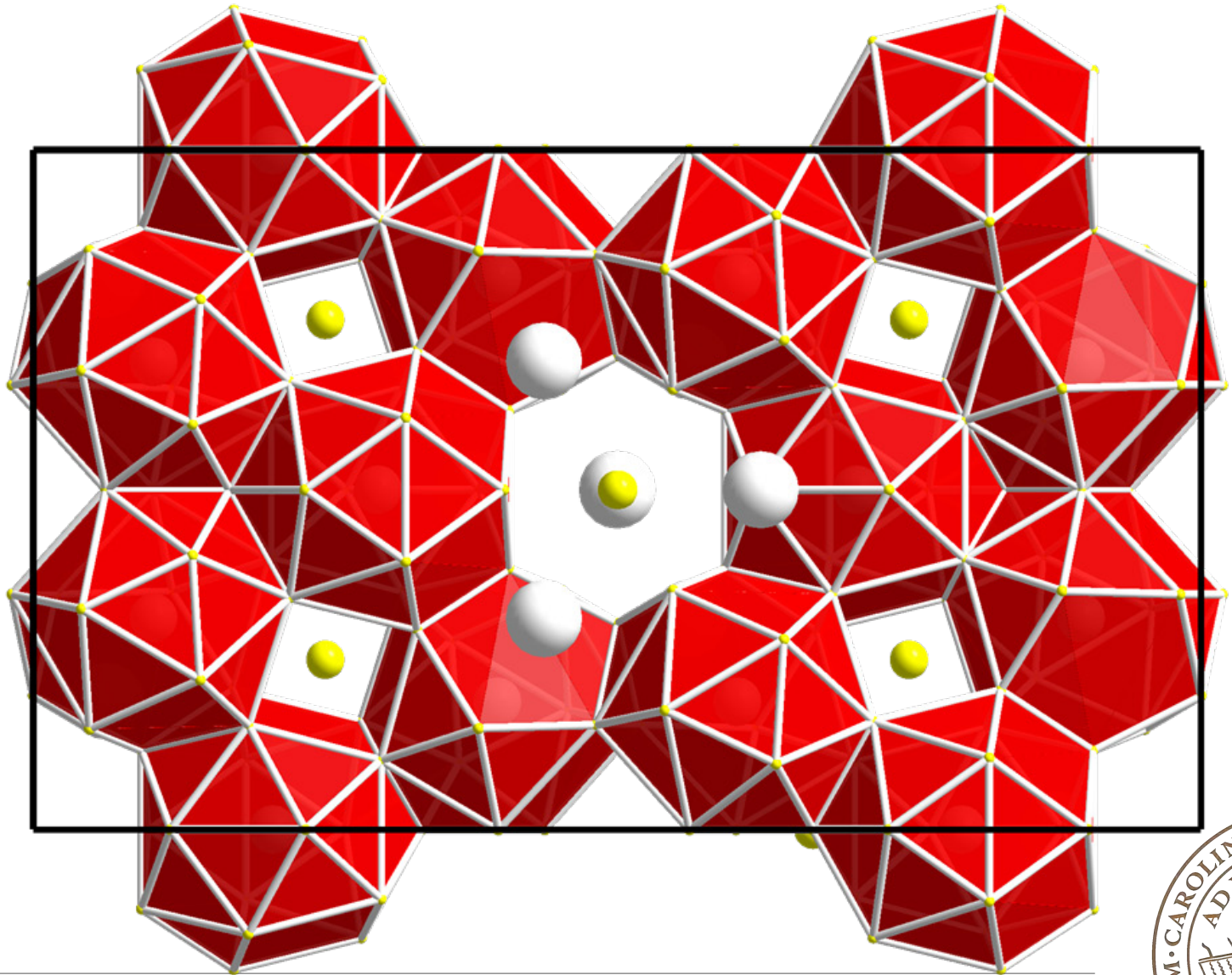




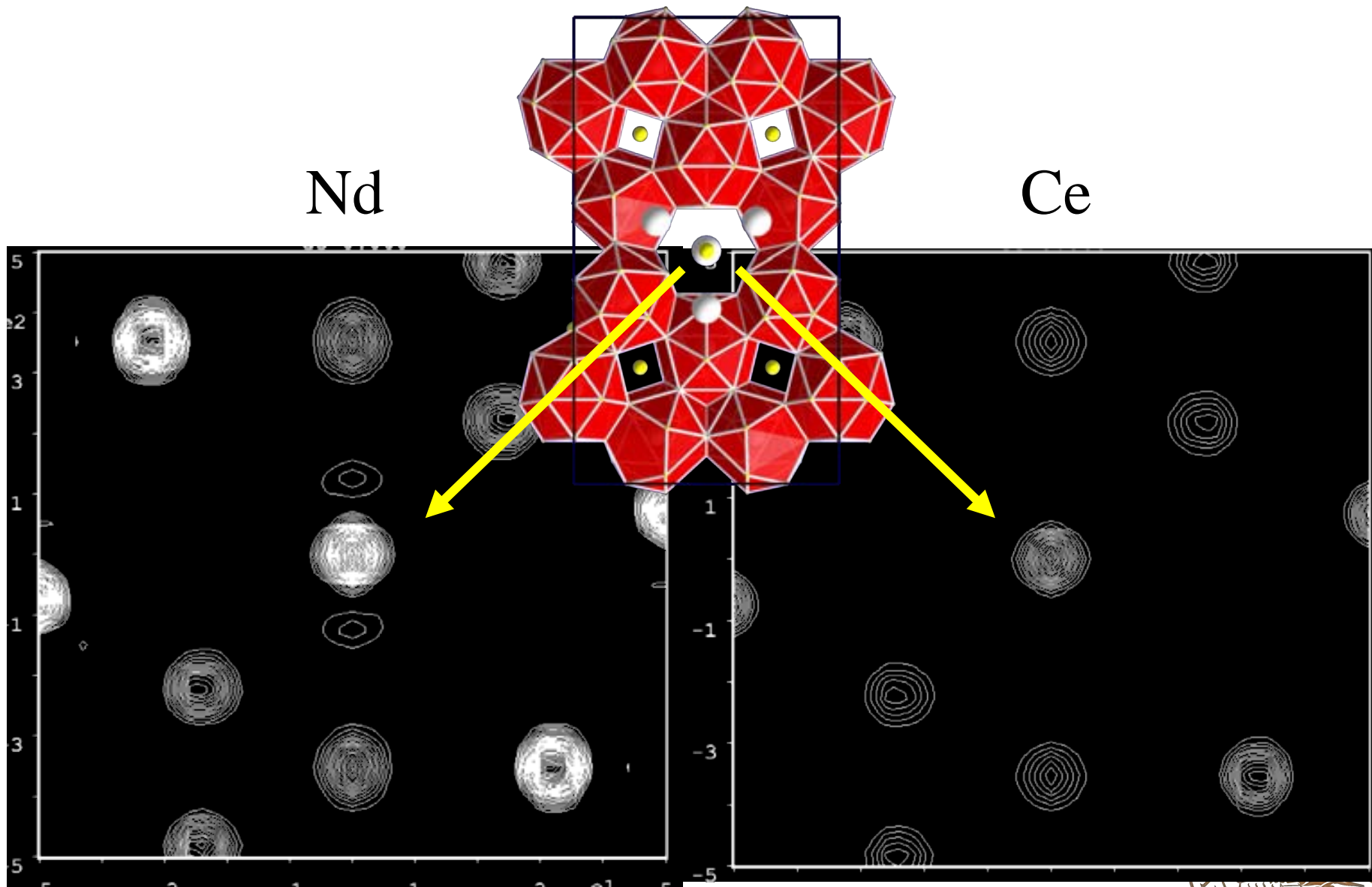
# Complex basic structure



# Complex basic structure



# Exchange mechanism I



# Exchange mechanism I

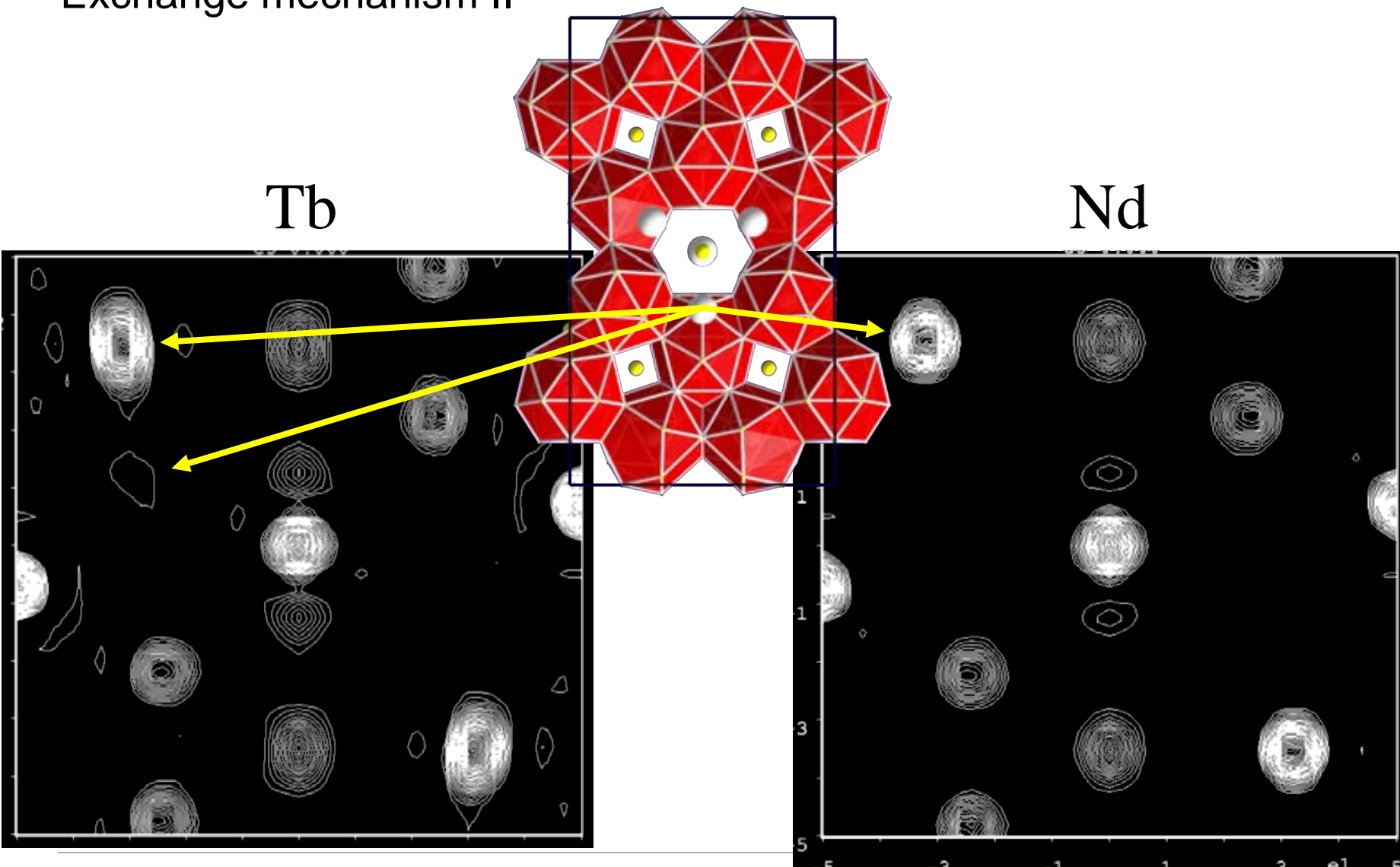
For Ce and Pr no exchange is found. For Nd it is found to some degree to make the composition  $\text{Nd}_{12.8}\text{Zn}_{58.4}$ .

For Yb, Sm, Gd and Tb it is found together with exchange mechanism II





# Exchange mechanism II



# Exchange mechanism II

**Mechanism II causes the symmetry lowering  $P6_3/mmc$  to  $P6_3mc$**

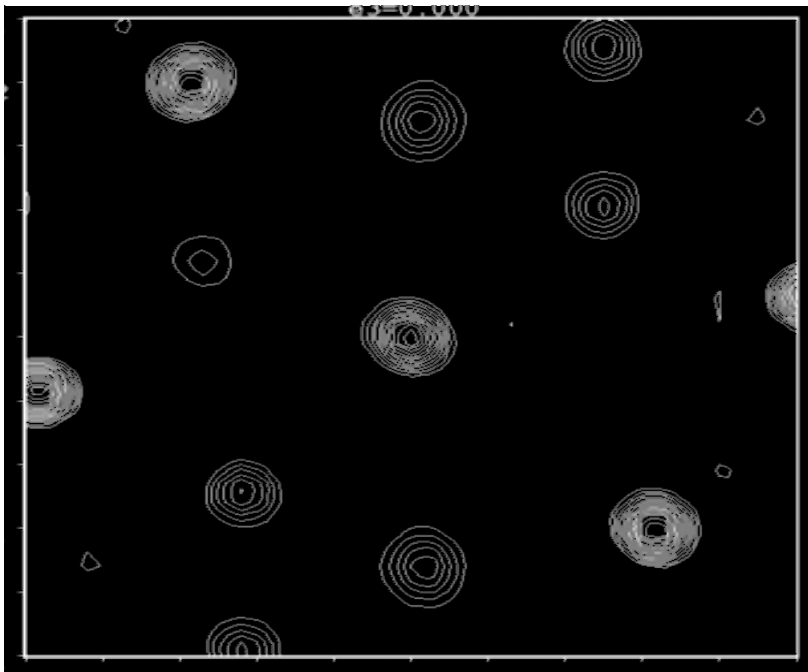
**It boosts Zn content further.**

**As occupancy of this position approaches 1/3, the next ordering kicks in**

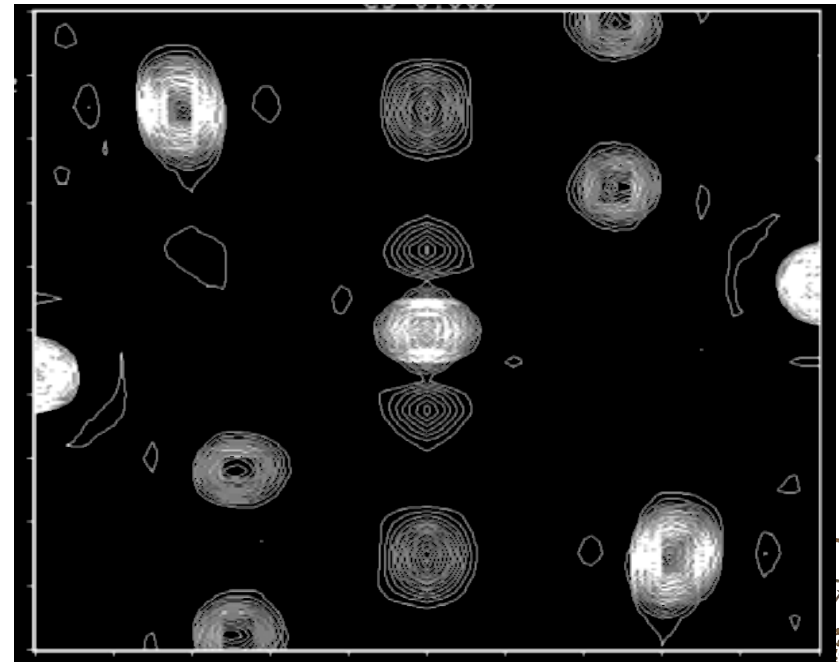


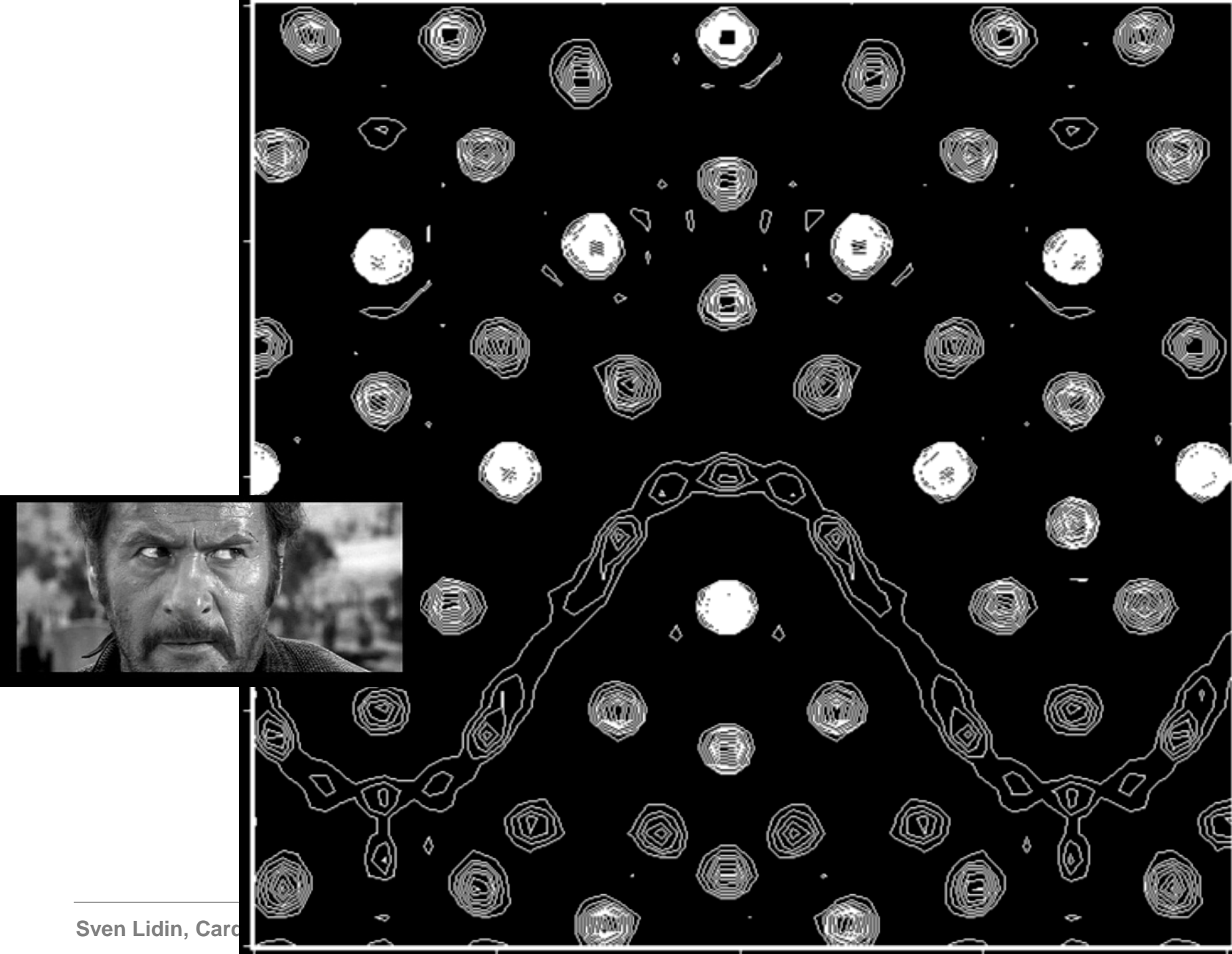
For fully ordered mechanism II, symmetry is reduced to  $P2_1$ . This applies to Gd and Tb. For Er, Tm, Lu additional disorder allows  $Pc2_1n$ .

Er



Tb (I)





Sven Lidin, Card



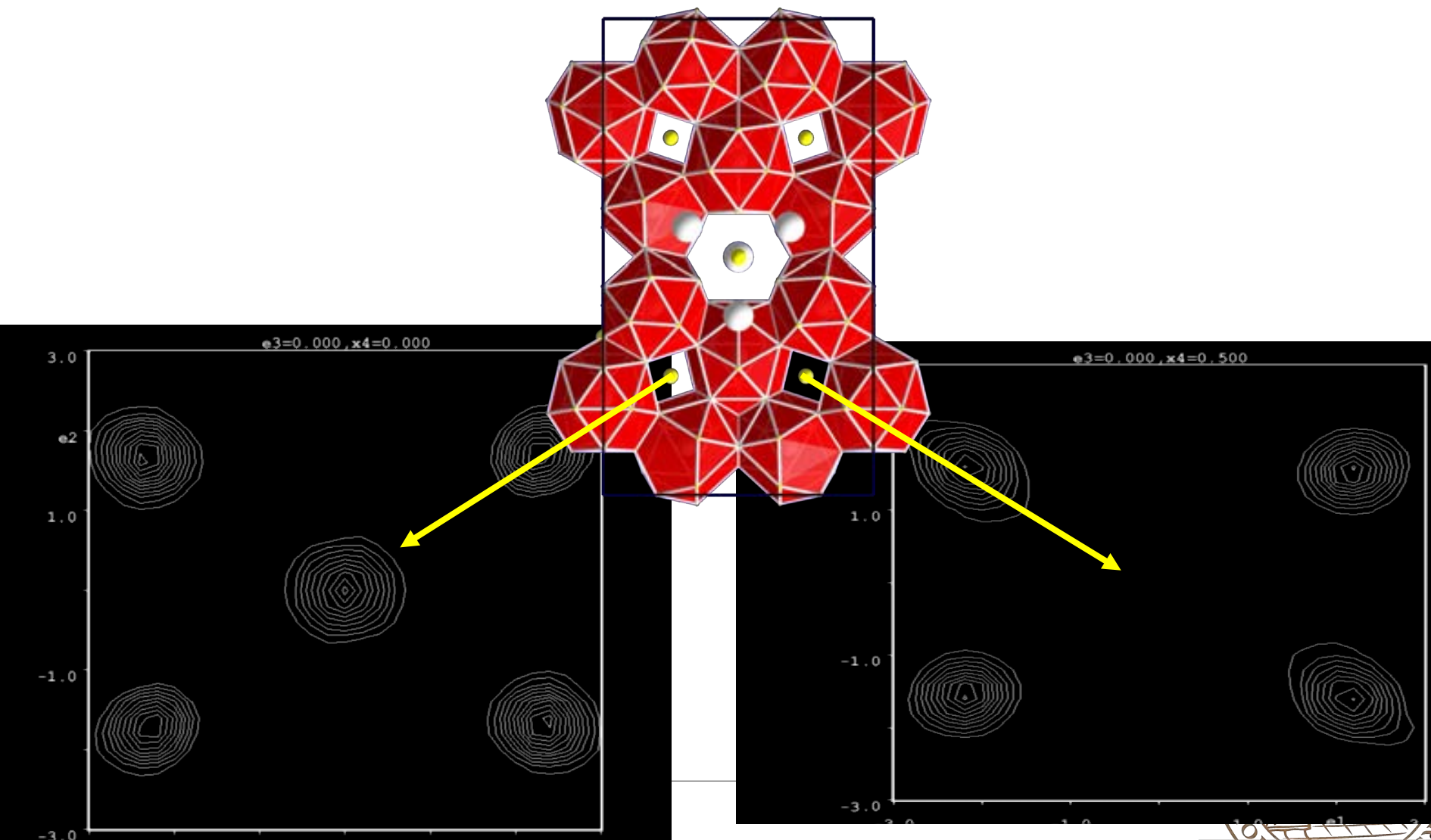
# Special cases

**Dy shows neither of the above mechanisms, but has an ordering all of its own.**

**Ho is very similar to Er and Tm but the additional disorder in the latter is resolved**

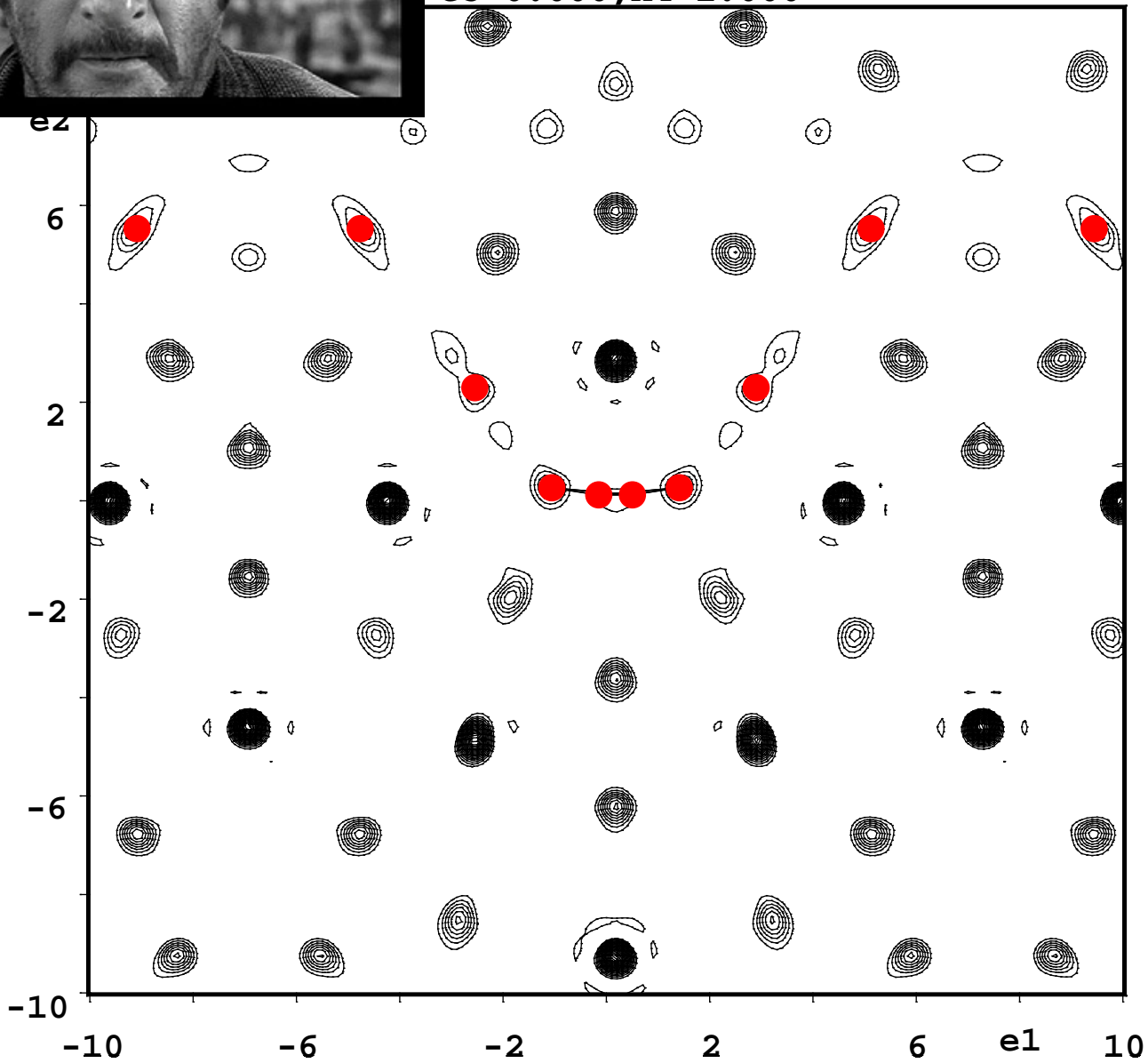


# Dy and exchange mechanism III





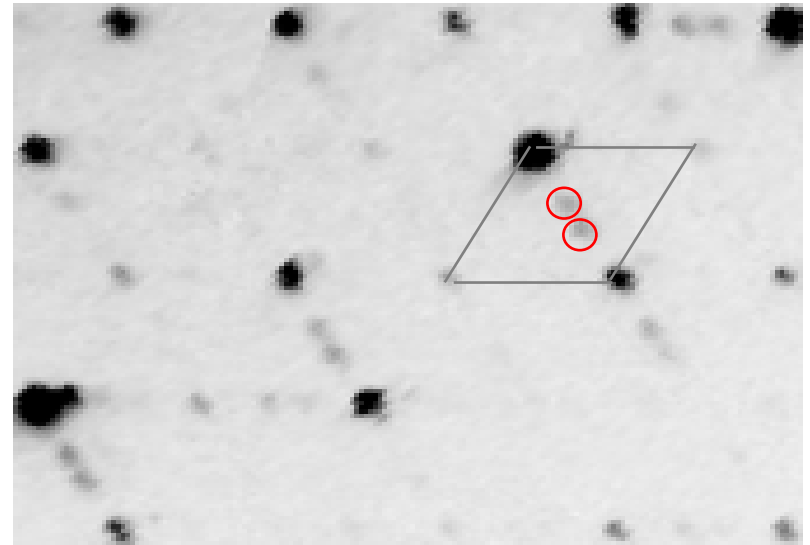
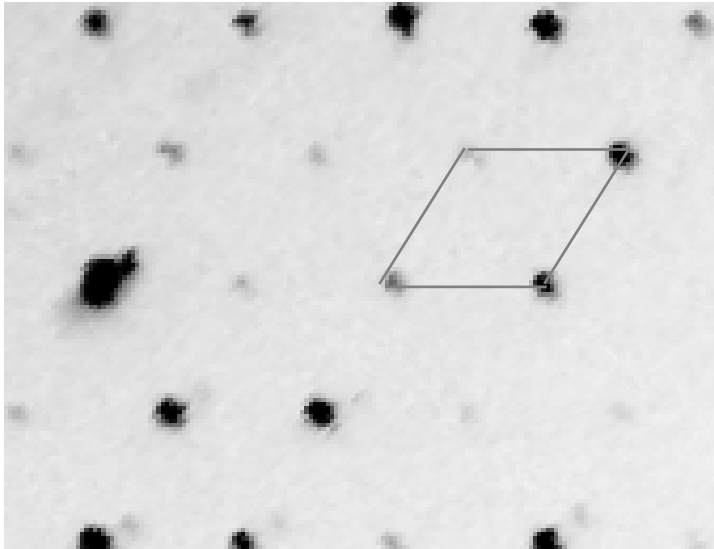
$e3=0.000, x4=1.000$



## Back to the Bad



# Remember $\text{Ce}_{13}\text{Cd}_{58}$



*hk0*

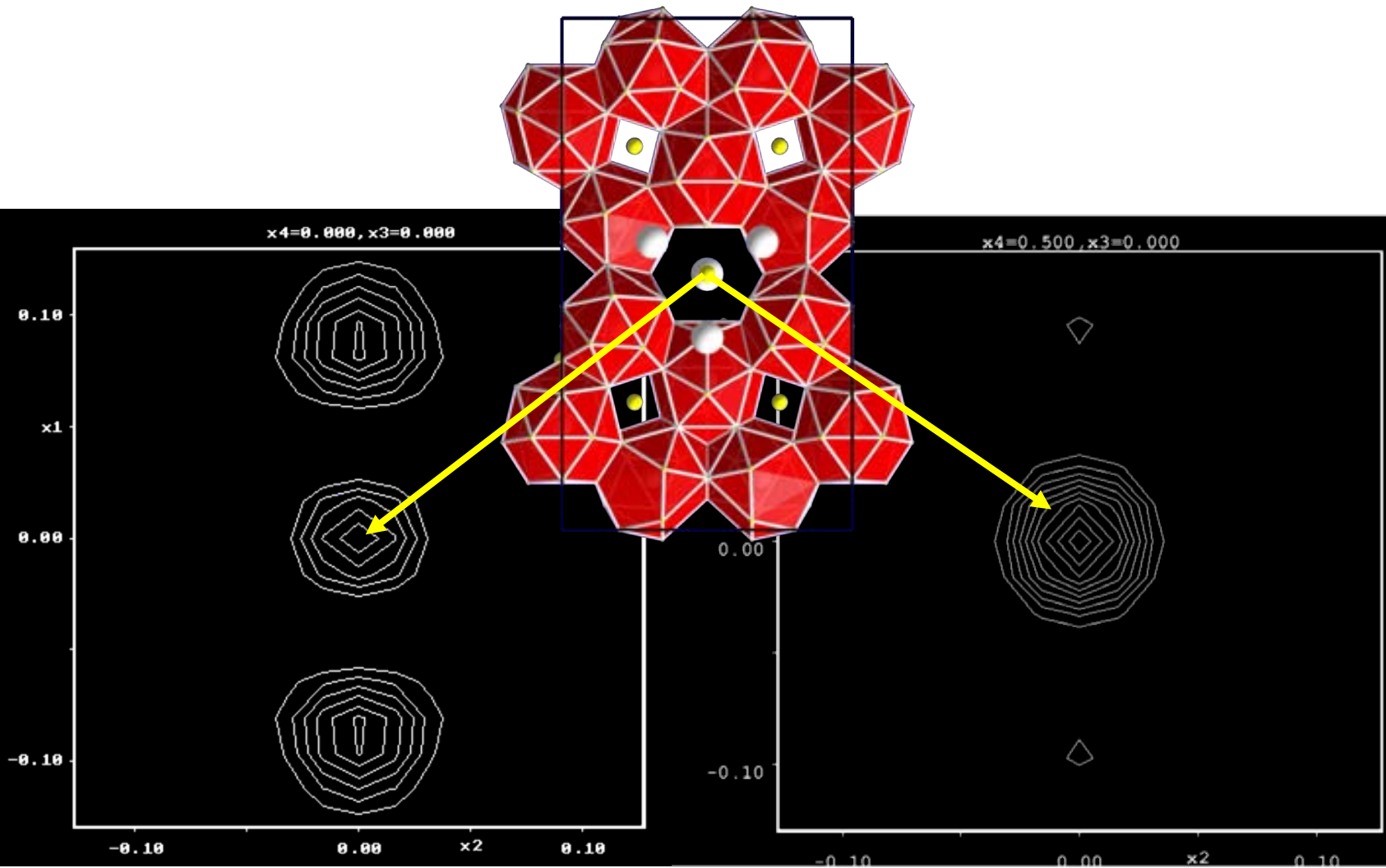
*hk1*

**This structure contains 32 independent positions.**

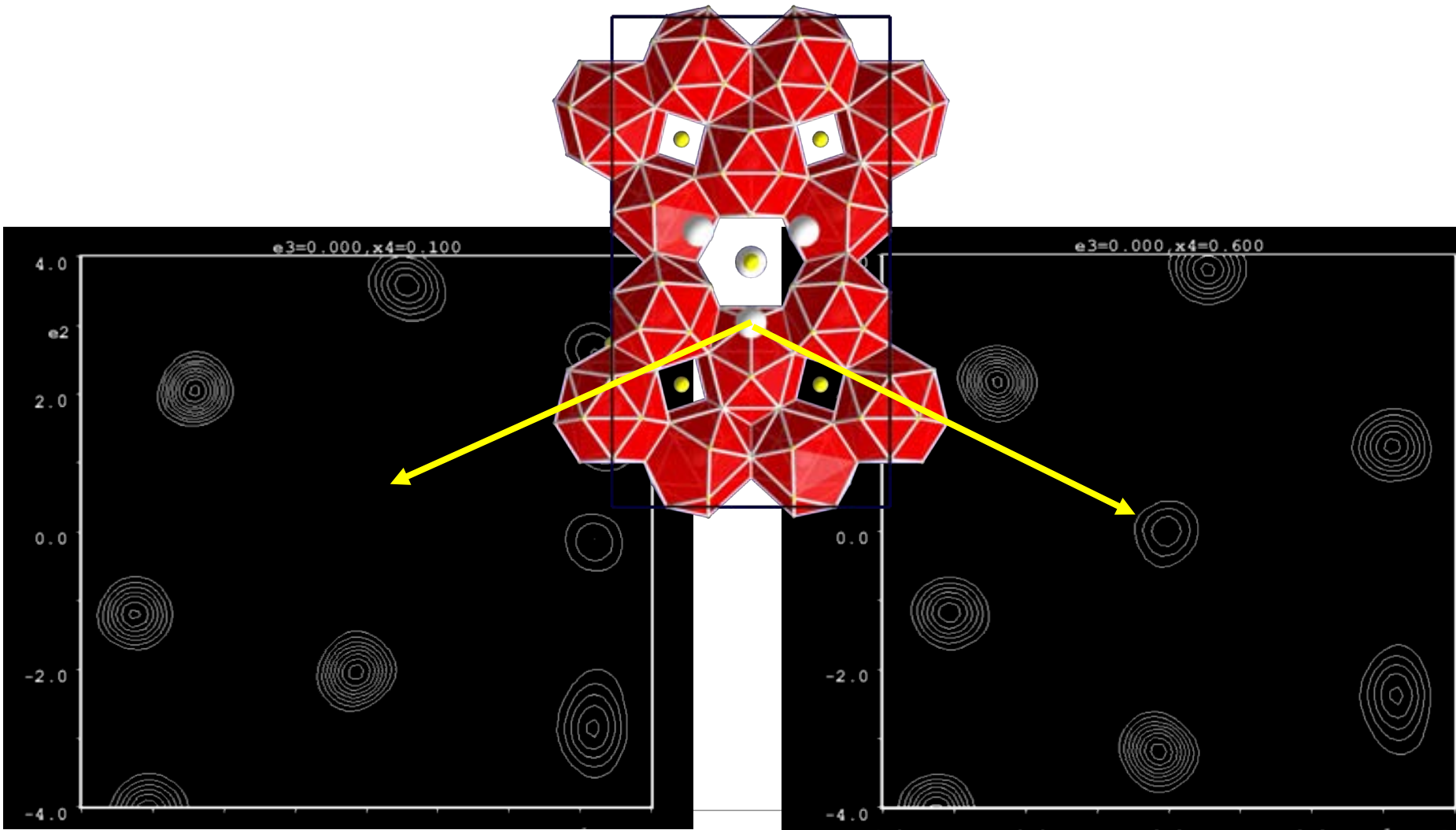
**The superspace group is  $\text{A}m\bar{m}a(00g)s00$**



# Exchange mechanism I

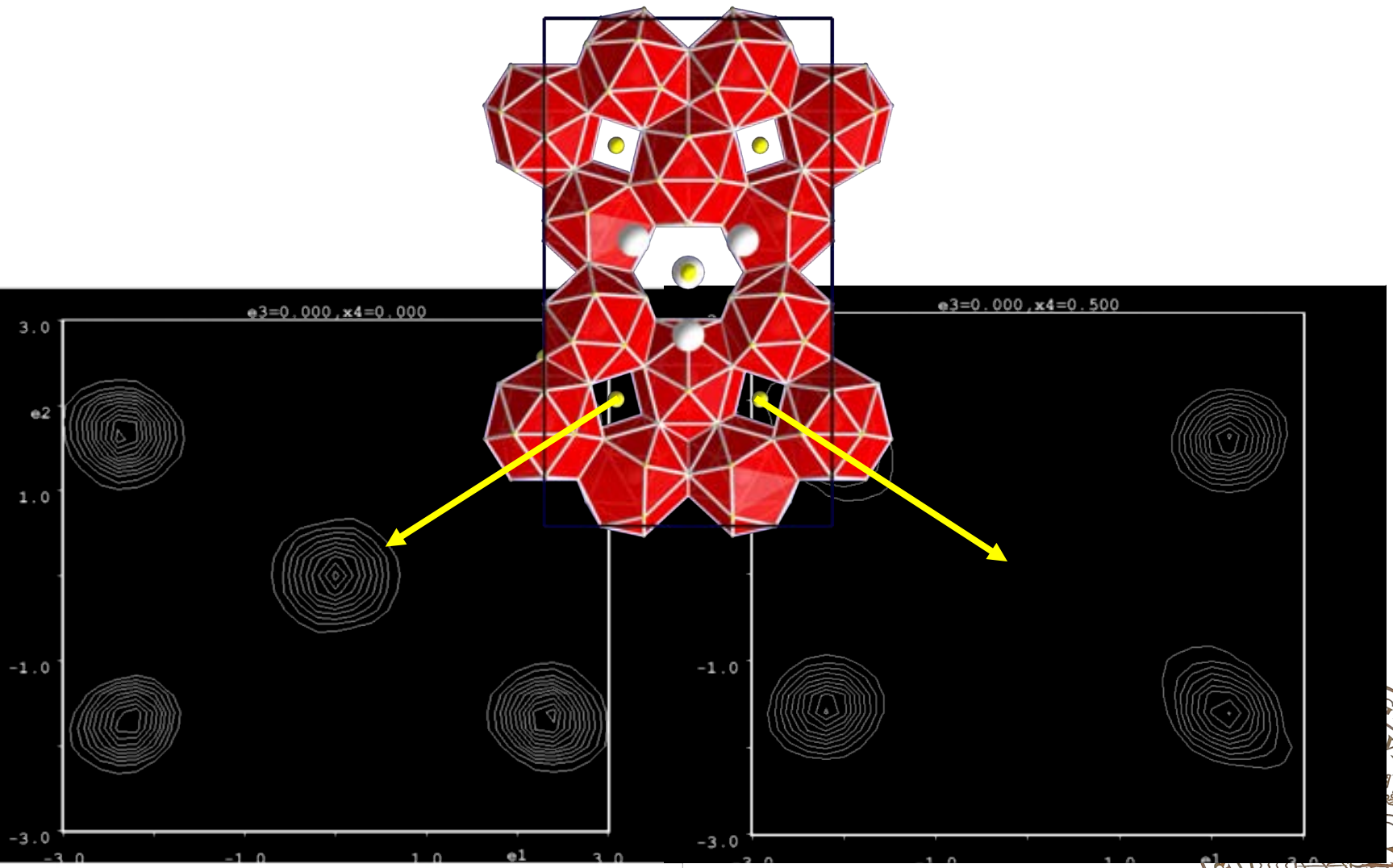


# Exchange mechanism II

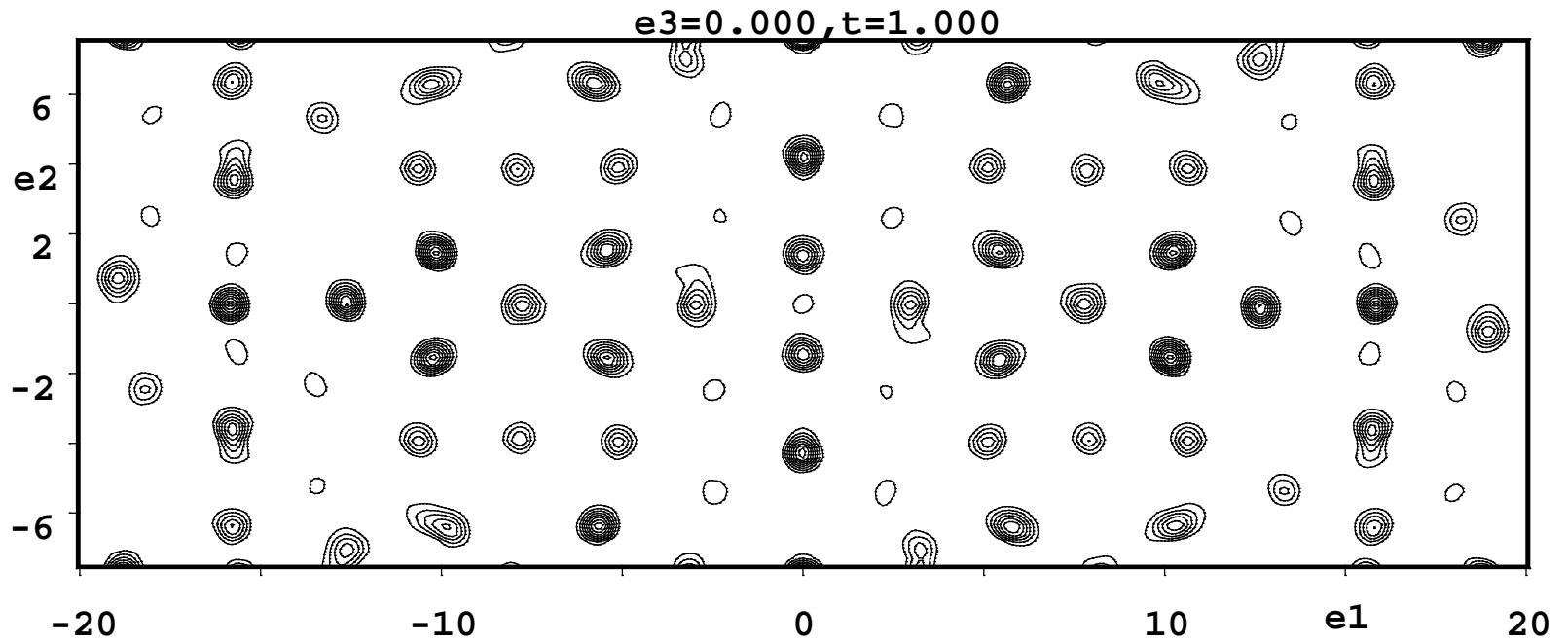




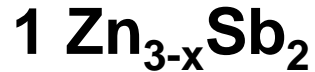
# Exchange mechanism III



Put it all together



# Examples

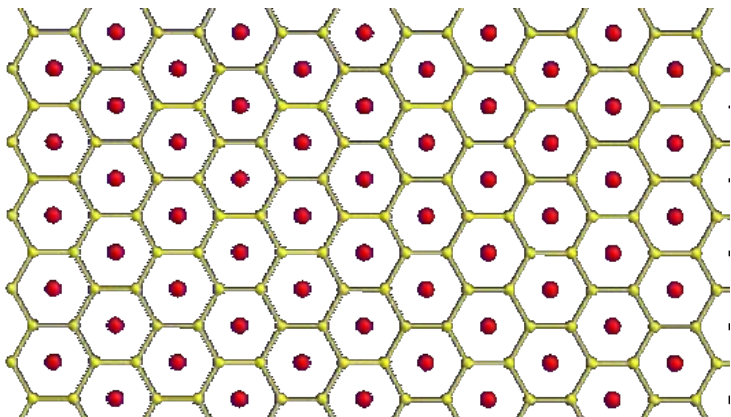


2 Stistaite

3 Onoratoite

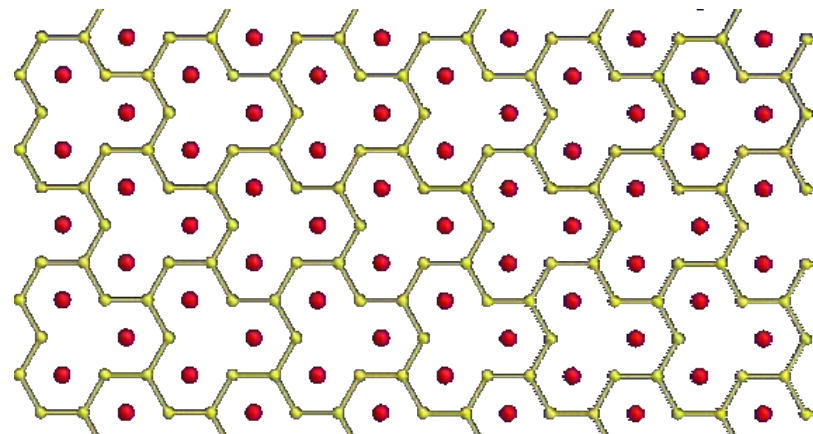


More  $AlB_2:XY_{2-q}$



$AlB_2 - P6/mmm - Cmmm$

$Yb_3Ge_5 - P6\bar{2}m - Cm2m$   
 $q = (1/3 \ 0 \ 0)$



$R_5X_8 - Pbam$   
 $q = (2/5 \ 0 \ 0)$





The centering condition should allow for the C-centering of the parent  $\text{AlB}_2$ , but also for the primitive cell of the 5:8 compound.

$$\alpha=0: \quad hklm \Leftrightarrow hkl \Rightarrow h+k=2n$$

$$\alpha=1/3: \quad hklm \Leftrightarrow 3h+m \ k \ l \Rightarrow 3h+m+k=2n$$

$$\alpha=2/5: \quad hklm \Leftrightarrow 5h+2m \ k \ l \Rightarrow 5h+2m+k=?$$

This shows that the m component is involved in the centering:  $h+k+m=2n$





**The a-glide  $\perp$  b is present even without the C-centering.  
This must be generated by an s-glide  $\perp$  b  $\Rightarrow$   
The superspace group is  $Xmmm(\alpha 00)0s0$ .**

**In many known compounds the q-vector takes the form  
 $q=(\alpha 0\gamma) \Rightarrow$   
The super space group must then be a subgroup of  
 $Xmmm(\alpha 00)0s0 \Rightarrow X2/m(\alpha 0\gamma)0s$**





## Composition

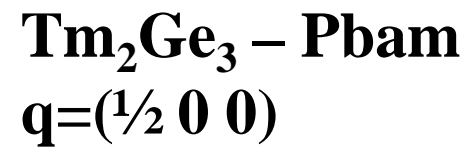
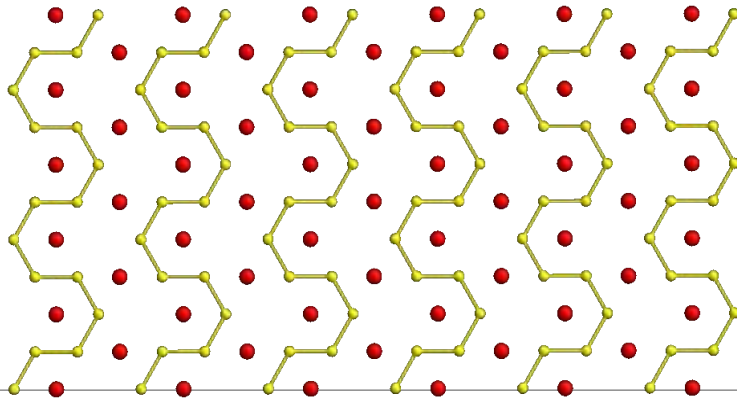
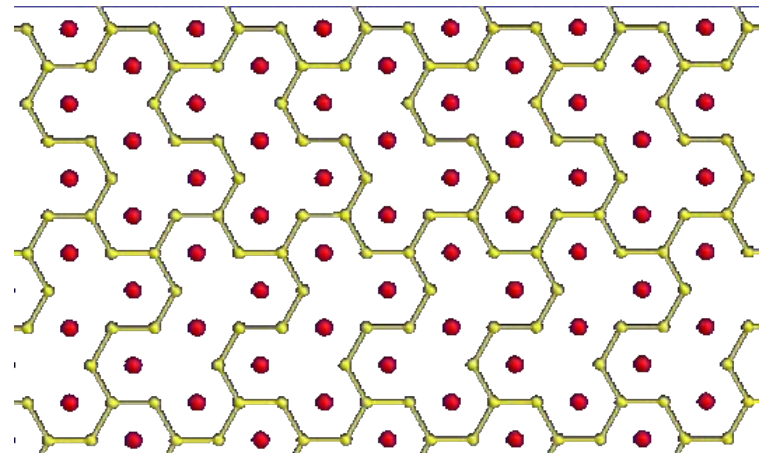
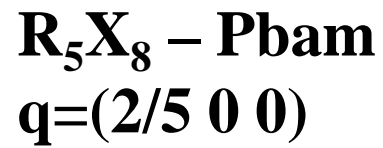
**The commensurate cases indicate that the composition is given by the q-vector according to  $\text{ReGe}_{2-\alpha x}$ .**

**Every second Ge atom is removed from a number of rows determined by  $q_x$ .**

**The limiting case is represented by  $\text{Tm}_2\text{Ge}_3$  and  $\text{Lu}_2\text{Ge}_3$ ,  $q_x=1/2$ .**



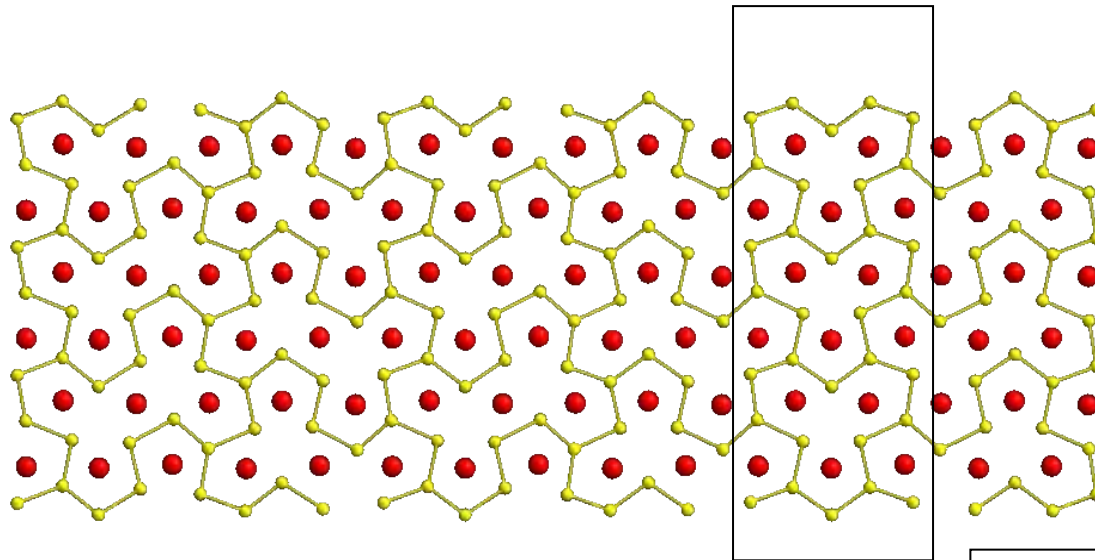
Limiting case



# Example – Lviv



# Example – DyGe<sub>2-x</sub>



$q < 0.4$

$q > 0.4$

